

# Crystallography



## Topics:

### 1. Image Formation (*what we see is not always accurate*)

Resolution / Wavelength (Amplitude, Phase) / Diffraction & Interference

Light Microscopy / EM / X-ray / (NMR)

### 2. Protein Data Bank (PDB)

Data mining and Protein Structure Analysis Tools

### 3. IYCr 2014 - Celebrating 100 years of X-ray Crystallography

### 4. X-Ray Crystallography – practical aspects

- Crystal Growth – Materials / Methods
- Crystal Lattices - Lattice Constants / Space Groups / Asymmetric Unit
- X-ray Sources – Sealed Tube / Rotation Anode / Synchrotron
- Theory of Diffraction – Bragg's Law / Reciprocal Space
- Data Collection – Methods / Detectors / Structure Factors
- Structure Solution – Phase Problem: MIR / MR / MAD
- Refinements and Models / Analysis and presentation of results

# Crystallography – Worlds of Wonder

## • Crystallography - What is it? How does it Work?

Early Years – historical overview

Demonstration of diffraction / image formation

Crystals + X-rays → record of Nobel Prizes

## → • Benefits of Crystallography to Society / IYCr 2014

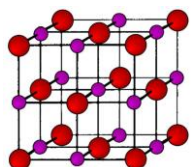
Crystallographic Awareness / Celebration / Training

IYCr: Summits (Africa / Asia / Latin America)

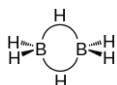
Crystal growth contests / Exhibits / etc.

Crystallography Discovery Kit for teachers & museums  
symmetry / crystal growth / diffraction

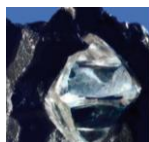
## Chemistry / Bonding



Sodium Chloride (NaCl)  
(a.k.a. Table salt)



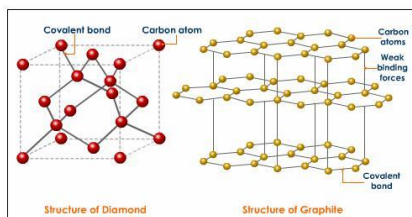
Bonding diagram of  
diborane ( $B_2H_6$ ) showing  
with curved lines a pair of  
3-center 2-electron bonds.



diamond  
Fd-3m  
Non-conductor



graphite  
P6<sub>3</sub>/mmc  
Conductor

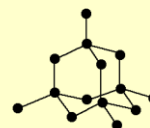


Structure of Diamond

Structure of Graphite

## Semiconductors

Silicon - a giant covalent structure

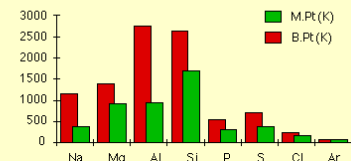


Silicon looks like a metal, but is a non-metal with the same structure as diamond. **Silicon is a semi-conductor.**

You can turn silicon into a **conductor** by **doping** it - mixing a small amount of an **impurity** into the silicon crystal.

## Variation in physical properties in period 3

### Melting and boiling points



### Four molecular elements

Phosphorus, sulphur, chlorine and argon are simple molecular substances with only van der Waals attractions between the molecules. Their melting or boiling points will be lower than those of the first four members of the period which have giant structures. The presence of individual molecules prevents any possibility of electrons flowing, and so none of them conduct electricity.

The sizes of the melting and boiling points are governed entirely by the sizes of the molecules.



a P<sub>4</sub> molecule



an S<sub>8</sub> molecule



a Cl<sub>2</sub> molecule

### Czochralski Crystal Growth

silicon melt    Introduction of seed crystal    crystal growth    ingot and remaining melt

Ceramic support for connected to pulling mechanism  
Cooled bell-pier enclosure  
Induction heater coil  
Crystal boule  
Insulating ceramics  
Molybdenum crucible containing melt components oxides

Seed  
Molten silicon  
Heating coils  
Crucible

Structure of zinc sulfide (ZnS) is similar to diamond.

### Transistors - tiny switches that can be triggered by electric signals. They are the basic building blocks of microchips (PNP/NPN).

Pure Silicon  
● Silicon nuclei

(+) P-Type Silicon  
● Boron nucleus  
hole

(-) N-Type Silicon  
● Phosphorus nucleus  
Extra electron

Structure of zinc sulfide (ZnS) is similar to diamond.

Doping of the Silicon Semiconductor Lattice

Group III Element Doping (p-type)  
Group V Element Doping (n-type)

Figure 2  
p-n Junction Region  
Silicon Tetrahedral Crystalline Lattice

### Basic Semiconductor Crystal Structure

Properties	Si	GaAs	InP	GaP	GaN	In <sub>0.53</sub> Ga <sub>0.47</sub> As
Band gap [eV]	1.12	1.42	1.35	2.26	3.39	0.75
Type	Indirect	Direct	Direct	Indirect	Direct	Direct
Lattice	fcc	fcc	fcc	fcc	hex	fcc

Zinc blende or sphalerite or Diamond structure

Wurtzite or hexagonal structure  
Red lines are not showing bonds.

**Wurtzite** is the name of the **b-ZnS** modification - the hexagonal high-temperature variant. The named after the French chemist C. A. Wurtz (\* 1817, † 1884),

### Materials Research

Crystallography underpins the development of practically all new materials, from everyday products like computer memory cards to flat television screens, cars and airplane components. **Crystallographers not only study the structure of materials but can also use this knowledge to modify a structure to give it new properties or to make it behave differently.** The crystallographer can also establish the new material's 'fingerprint'. A company can then use this 'fingerprint' to prove that the new substance is unique when applying for a patent.

Crystallography helps to determine the ideal combination of aluminum and magnesium in alloys used in airplane manufacture. Too much aluminum and the plane will be too heavy, too much magnesium and it will be more flammable.

© Shutterstock/IM\_photo

**Medicine**

**Penicillin**

Penicillin kills bacteria by interfering with aminopeptidase, an enzyme responsible for making bacteria cell wall. Human and mammals do not have this enzyme.

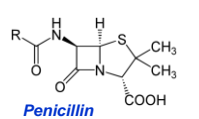
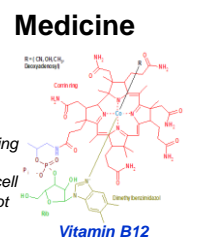

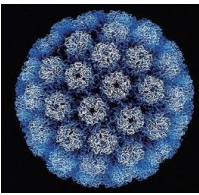
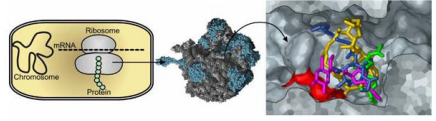

**Vitamin B12**

Structure of DNA – human genome, genetic diseases

SV40 (simian virus) structure, has been linked to mesothelioma.

Chloramphenicol, Tiamulin, Dalofopristin, Chloramphenicol

Chloramphenicol, tiamulin and other antibiotics target the peptidyl transferase center (PTC) on the bacterial ribosome.

The Nobel Prize in Physiology or Medicine 1945  
Sir Alexander Fleming, Ernst B. Chain, Sir Howard Florey





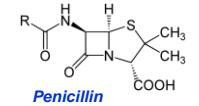
**Alexander Fleming and Penicillin: The Accidental Discovery?**

**The Nobel Prize in Physiology or Medicine 1945**

Sir Alexander Fleming, Ernst Boris Chain, Sir Howard Walter Florey

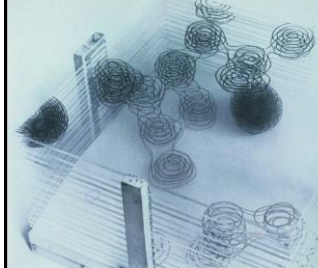
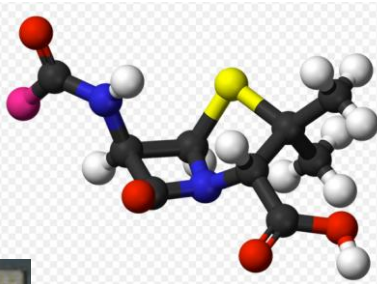
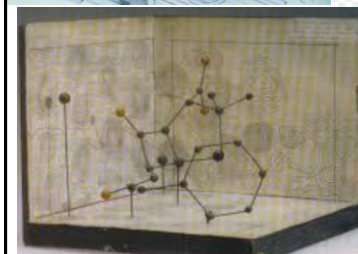
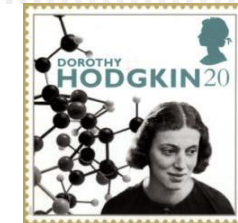
The Nobel Prize in Physiology or Medicine 1945 was awarded jointly to Sir Alexander Fleming, Ernst Boris Chain and Sir Howard Walter Florey "for the discovery of penicillin and its curative effect in various infectious diseases".

**Penicillin**

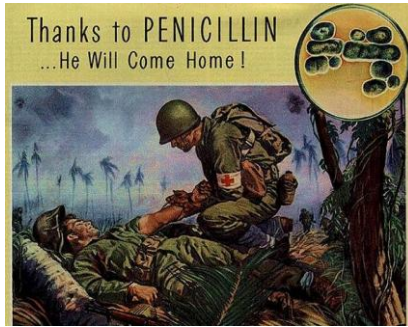
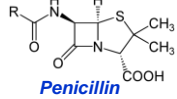
**Brief History of Penicillin**

- Alexander Fleming** (Scottish scientist) fought in **World War I**. His battlefield experience showed him how dangerous bacteria could be to human life. After the war he focused on finding a chemical that would stop bacterial infection.
- In the **Fall of 1928**, Fleming had prepared **Staphylococcus** on several plates and forgot to put them in the incubator before he went on vacation. When he returned from vacation, he discovered that one of the plates was contaminated with molds. This particular mold strain (later identified to be **Penicillium notatum**) was a **good producer of penicillin**.
- In 1935, **Howard Florey** working on penicillin. By **May 1940**, the team produced enough penicillin to test on infected animals for the first time. Eight mice were infected with a lethal dose of *Staphylococcus*. One hour later, four of them were injected with penicillin and the other four were left without treatment. All four mice that did not receive penicillin died in less than 24 h. All four mice treated with penicillin were healthy. Florey proclaimed, "it looks like a miracle".
- The first batches of this new wonder drug became available in 1943 and were reserved for military use. The government recruited 21 chemical companies to produce penicillin. From January to May 1943, only 400 million units of penicillin were made; by the time the war ended, US companies were making 650 billion units a month.
- Penicillin kills bacteria by interfering with aminopeptidase, an enzyme responsible for making bacteria cell wall. Human and mammals do not have this enzyme.



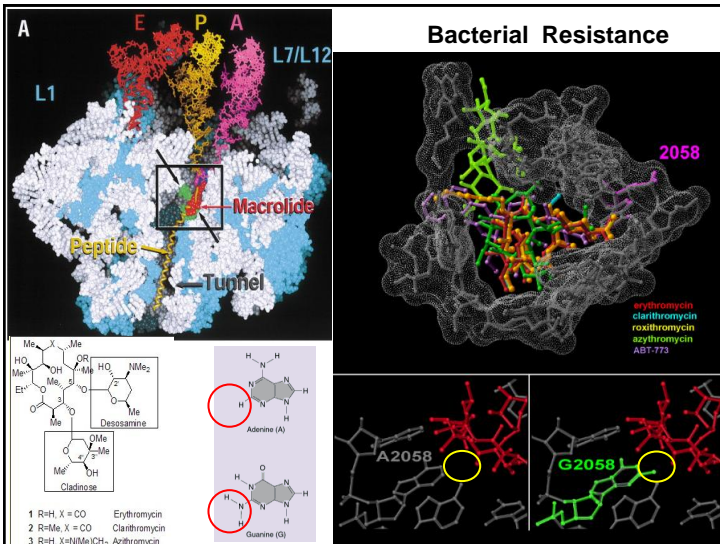
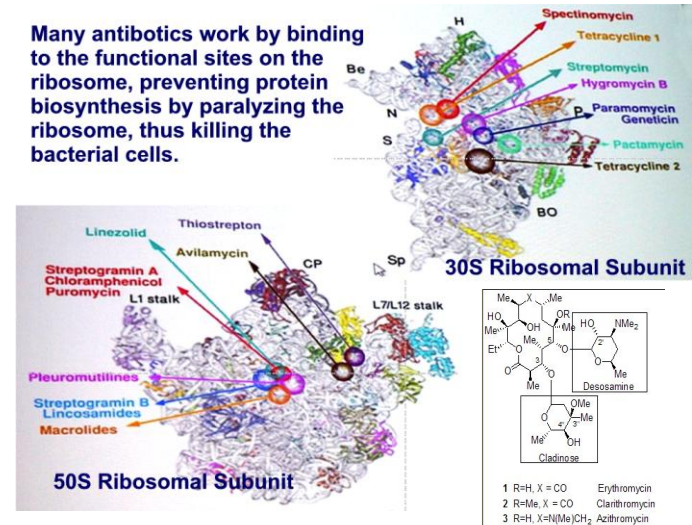
# Medicine: The Good Old Days...



**modern headlines:** The ticking time bomb...  
The serious threat...  
escalating **antibiotic resistance**...  
untreatable bacterial infections...

Doug Mitchell, Univ. of Illinois at Urbana-Champaign

Many antibiotics work by binding to the functional sites on the ribosome, preventing protein biosynthesis by paralyzing the ribosome, thus killing the bacterial cells.



## Human Genome Project

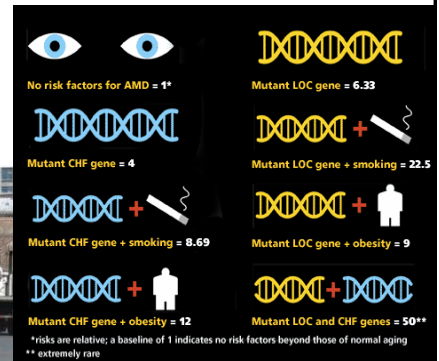


### Age-related macular degeneration (AMD)



### Nature versus nurture

Using data mining from the **Human Genome Project**, researchers traced the genetic roots of AMD to inherited mutations in two genes known as complement factor H (CFH) and LOC387715, and correlated that with other risk factors.

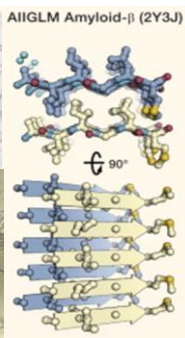
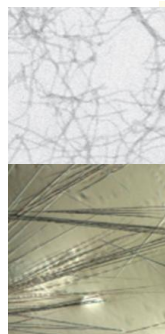
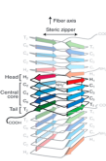


## Amyloid Related Conditions

**Amyloid**  
(disease / protein)  
**Alzheimer's / Tau**  
**Diabetes II / Amylin**

**Prion (transmissible)**  
(disease / protein)  
**Creutzfeldt-Jakob / PrP**  
**Mad Cow / PrP**

**Amyloid-like**  
(disease / protein)  
**Parkinson's /  $\alpha$ -synuclein**  
**LouGehrig's / SOD**

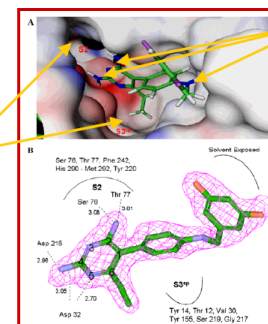
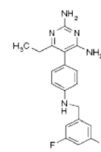


### Steric Zipper Hypothesis:

- >120 segments of amyloid-forming proteins form micro-crystals with a common flat sheet structural motif.
- Zipper-forming segments can seed parent proteins into fibers
- Amyloid-inhibitors are designed to block steric zipper fibers**

## Crystallography in Drug Design

Renin inhibitors are a group of pharmaceutical drugs used primarily in treatment of hypertension (high blood pressure). The binding orientation of a lead compound to inhibit Renin was determined by X-ray crystallography.

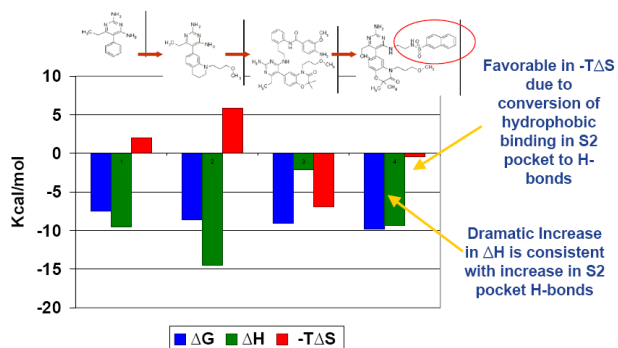


The unoccupied hydrophobic S2 and S3 pockets are opportunities to enhance favorable  $\Delta S$

favorable  $\Delta H$  is consistent with the strong network of hydrogen bonds.

## Crystallography in Drug Design

**Renin inhibitors:** Chemists use the information from the X-ray structure to improve binding of the lead compound. Modeling suggests substituting the aryl-benzamide with an aryl-sulfonamide to improve H-bonding to improve its fit on the target.



## Renin Inhibitor Binding Affinity Improved from $3.6 \times 10^{-6} \text{ M}$ to $79 \times 10^{-9} \text{ M}$ (46X)

Improved binding means less of the drug is needed, resulting in lower manufacturing costs per dose and a reduction of side effects.

- S3 Pocket – Ether addition improved enthalpy due to van der Waals bonds
- S2 Pocket – Aryl-Sulfonamide improved binding enthalpy while retaining hydrophobic advantage



GE imagination at work



## Space Exploration



The **Curiosity rover** used X-ray crystallography in October 2012 to analyze soil samples on the planet **Mars!**

NASA had equipped the rover with a diffractometer. The results suggested that the Martian soil sample was similar to the weathered basaltic soils of Hawaiian volcanoes.

Photo: NASA

## Crystallography and Chocolate

**Cocoa butter**, the most important ingredient of chocolate, **crystallizes in six different forms** but only one (form V) melts pleasantly in the mouth and has the surface sheen and crisp hardness that make it so tasty.

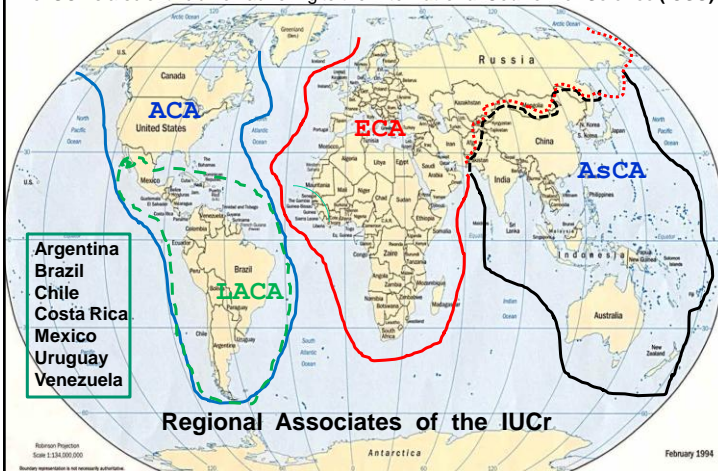
Crystal form	Formation conditions	m. p. (°C)
I	rapid cooling of the melt	17.3
II	rapid cooling of the melt at 2 °C/min	23.3
III	crystallization of the melt at 5–10 °C, converts into II at 5–10 °C	25.5
IV	crystallization at 16–21 °C	27.3
V ★	slow crystallization of the melt	33.8 (93 °F)
VI ★	from form V after several months at RT	36.3 (98 °F)



Unfortunately, this 'tasty' crystal form is not very stable so it tends to convert into the more stable form (VI), which is dull, has a soft texture and melts only slowly in the mouth, producing a coarse and sandy sensation on the tongue. The conversion is slow, but if chocolate is stored for a long time or at a warm temperature, it can develop a 'bloom,' a white, filmy residue that results from recrystallization. Chocolate-makers thus have to use a sophisticated crystallization process to obtain the most desirable crystal form of cocoa butter in chocolate. Adding milk fat retards the conversion so that the V→VI transition is less often observed in milk chocolate!

## IUCr - International Union of Crystallography

The IUCr is a scientific union adhering to the International Council for Science (ICSU)



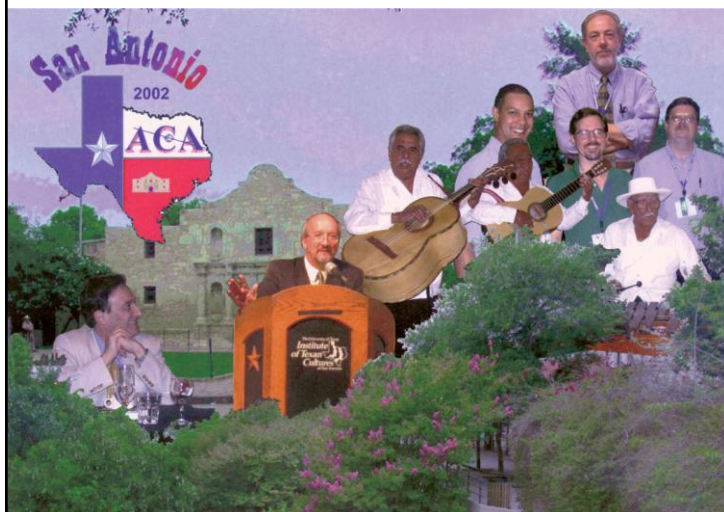
Each country is represented by its national committee – USNC/Cr



USNC/Cr - November 2001

Guest - Jack Marburger (White House Science Adviser, Dir. OSTP)

Regional Associates hold annual conferences - ACA Council



University of Texas at Austin – ACA Presidents



International Union of  
**CRYSTALLOGRAPHY**

IUCr Executive Committee 2014-2017

At the twenty-third Congress and General Assembly of the International Union of Crystallography, Professor Martin L. Hackett was elected as the new President of the IUCr. The photograph shows the Co-Chair of the Finance Committee and the Executive Secretary alongside Professor Hackett and the other members of the new Executive Committee for the triennium 2014-2017.

Back row: M. J. Cooper (Co-Chair, IUCr Finance Committee), M. H. Drenth (Executive Secretary), Executive Committee: J. M. Oun, R. Kozel, M. Takata, W. Depireux, S. Garcia-Ortega. Front row: H. Dabkowska, L. Van Meervort (General Secretary) and Co-Chair, M. L. Hackett (President), A. M. Glazer (Vice President), G. B. Storz (Immediate Past President).

Please join the IUCr in welcoming the new Executive Committee and thanking those members retired.

**The IUCr Intl. Congress 2014 - Montreal**

Bragg Symposium: Celebrating 100 years of X-ray crystallography - The University of Adelaide, 6th December 2012





opening ceremony  
unesco building  
paris  
20-21 january 2014

**IYCr2014 Opening Ceremony**  
ADMISSION TICKET

Paris – UNESCO Headquarters –  
Room 1  
7 Place de Fontenoy, 75007 Paris  
20-21 January 2014

**TIMELINES OF CRYSTALLOGRAPHY**

Use of X-rays to determine crystal structure  
**Nobel Prize in Physics 1915**  
Sir William Henry Bragg and Sir William Lawrence Bragg  
for their services in the analysis of crystal structure by means of X-rays.

**Timelines of Crystallography**

1. Click on the buttons to show or hide timelines (up to 5 can be shown side by side)

2. Drag the timeline or select a date: 1500 | 1600 | 1700 | 1750 | 1800 | 1850 | 1900 | 1950 | 1975 | 2000 | 2014

3. Show ("filter") or highlight entries containing a given word

4. Discovery of X-rays

5. Discovery of the characteristic Röntgen radiation of the elements

6. Use of X-rays to determine crystal structure

7. Diffraction of X-rays by crystals

<http://www.iycr2014.org/timeline>

- Experiments on X-ray diffraction
- Theory of X-ray diffraction
- 2θ sin theta = n lambda
- First structure determination
- Reciprocal lattice
- Corrected intensities
- Bragg law
- Contribution to the interpretation of X-ray diffraction patterns
- Spinel structures
- Integrated reflections: X-ray scattering by imperfect crystals
- Determination of unit-cell content
- Fourier series to represent electron density
- Powder photographs

IUCr-UNESCO  
**openLab**  
openFactory  
<http://www.iycr2014.org>

together bringing nations  
summit meetings

bloemfontein  
campinas  
karachi

**Latin American Summit - Campinas, Brazil September 22-24, 2012**

[pages.cnpem.br/iycr2014-lasummit](http://pages.cnpem.br/iycr2014-lasummit)





**Education / Celebration for IYCr 2014**

**Crystallography Discovery Kit for K-12 teachers / children's museums**

i) Crystal Jars Kit



ii) Symmetry and Lattices




**Molecular Structure Laboratory**

**Wisconsin Crystal Growing Contest**

Updated: December 18, 2013

**Announcement**

To celebrate the International Year of Crystallography 2014, the Molecular Structure Laboratory of the UW-Madison Chemistry Department has launched the Wisconsin Crystal Growing Competition to be held April-May 2014 among Wisconsin high school students.

This is an exciting scientific competition as well as a fun, hands-on experience. High schools are provided with materials on a first come first serve basis. Instructions on how to grow crystals are provided on the web. The objective is to grow the *biggest and highest quality single crystal*. The contest is described in the [Handbook](#).

The winners will compete in the National Crystal Growing Competition. Additionally, everyone has a chance to compete in the [International Crystal Growing Competition](#).

**For 2014 the material used for the crystal growing competition is cupric sulfate,  $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$  (copper (II) sulfate pentahydrate, or 'bluestone').**

*This material is chosen because it produces large beautiful blue crystals, which are neither too easy nor too difficult to grow. Cupric sulfate was also the compound used in the first X-ray diffraction experiment by Max von Laue in 1912.*

*It is available free of charge on a first come first serve basis. Each participant or team is eligible for 200g of pure cupric sulfate.*

WHAT STARTS BEING CHANGED THE WORLD  
THE UNIVERSITY OF TEXAS AT AUSTIN

General Information Schedule K-12 Connections Promotional Resources Media Gallery Site Map

**SAVE THE DATE: Saturday, March 1, 2014**

**EXPLORE UT**  
THE BIGGEST OPEN HOUSE IN TEXAS

**Saturday, March 1, 2014**  
**11 a.m. to 5 p.m.**  
Free. No registration required.



Explore UT 2014 Crystals & Crystallography - HG2014

### Growing Crystals at Home

It is relatively easy and fun to grow crystals of common chemicals at home with a minimum of time and effort. Three of the favorite crystals to grow at home are alum (a common spice that can be obtained at most grocery stores), borax (common detergent), and copper sulfate (used as a root killer). Crystals grow by a process termed nucleation from saturated or supersaturated solutions.

**Step 1: Buy Alum at grocery store**      **Step 2: Make a saturated solution**      **Step 3: Grow seed crystal**      **Step 4: Add seed crystal to supersaturated solution to continue its growth**

Alum crystal

*How much material it takes to make a saturated solution depends on the solubility of the substance. Most materials are more soluble in hot solutions, but the range varies a lot. For example, the solubility of common table salt (NaCl) increases by less than 10% between room temperature and the boiling point of water, whereas the solubility of copper sulfate increases by over 4-fold over this same temperature range (see graphs below taken from Fig 1.1 from crystal growing webpage).*

NaCl (NaCl) Crystals      Copper Sulfate Crystals

Formula:  $Na_2Cl_2$       Formula:  $CuSO_4 \cdot H_2O$

$Fm\bar{3}m, a = 5.64 \text{ \AA}$        $o = 6.11 \text{ \AA}, b = 10.71 \text{ \AA}, c = 5.96 \text{ \AA}$   
 $a = 82.4^\circ, b = 107.3^\circ, \text{ and } \gamma = 102.6^\circ$

There are many web links and youtube videos to show you how to grow crystals at home. Below are just a few links to detailed steps on how to grow crystals at home. The alum crystal shown below at right was grown in less than 2 days.

Alum Crystal

Explore UT 2014 Crystals & Crystallography - HG2014

### Symmetry

**Bilateral symmetry**, where the left and right sides are mirror images of one another, is common in nature such as seen in butterflies and snowflakes - and has also been a common feature of architecture.

**2-Fold Rotations**

180° rotation about a vertical axis      180° rotation about a horizontal axis

**Mirror Planes**

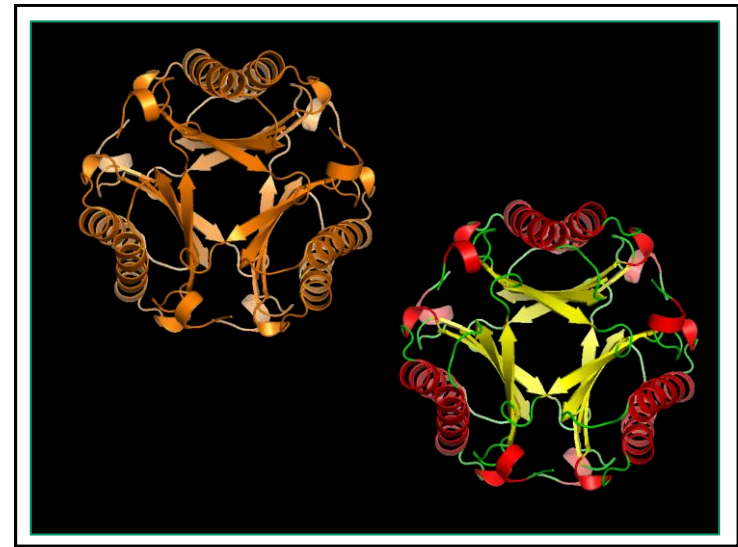
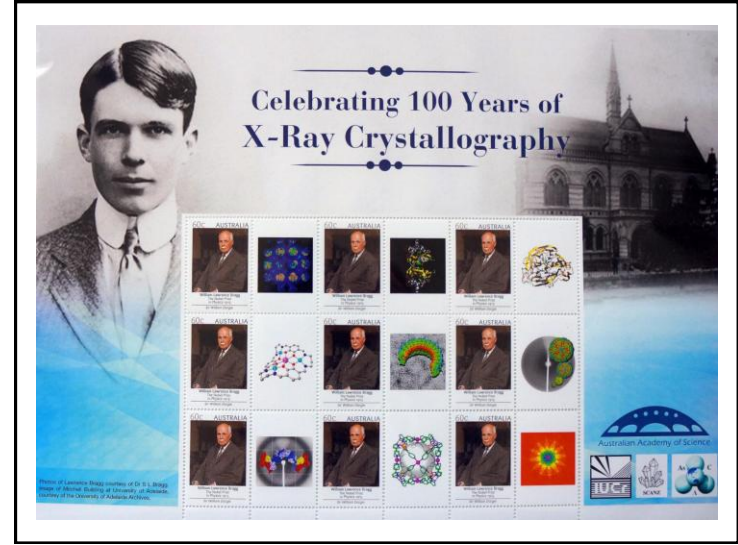
Vertical      Horizontal

Now consider the alphabet shown below:

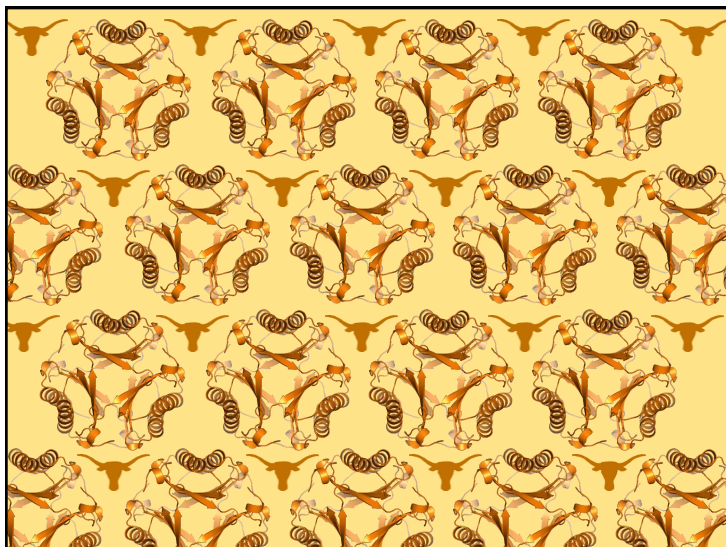
- How many letters have no symmetry? \_\_\_\_\_ Place an "X" in the upper left box of letters with no symmetry.
- How many letters have a vertical axis of symmetry? \_\_\_\_\_ Draw a vertical arrow indicating the symmetry axis.
- How many letters have a horizontal axis of symmetry? \_\_\_\_\_ Draw a horizontal arrow indicating the symmetry axis.
- How many letters are symmetrical about a 2-fold rotation axis perpendicular to the plane of the page? \_\_\_\_\_ Place a "□" mark in the upper right box of those letters with a perpendicular 2-fold rotation axis, and a "dot" indicating the location of the rotation axis.
- Now identify the symmetry present in the two words in the last two frames. Answers are given on other slide, but note results can vary with the font used!



IUCr 2014 – Display of 3D Printed Models





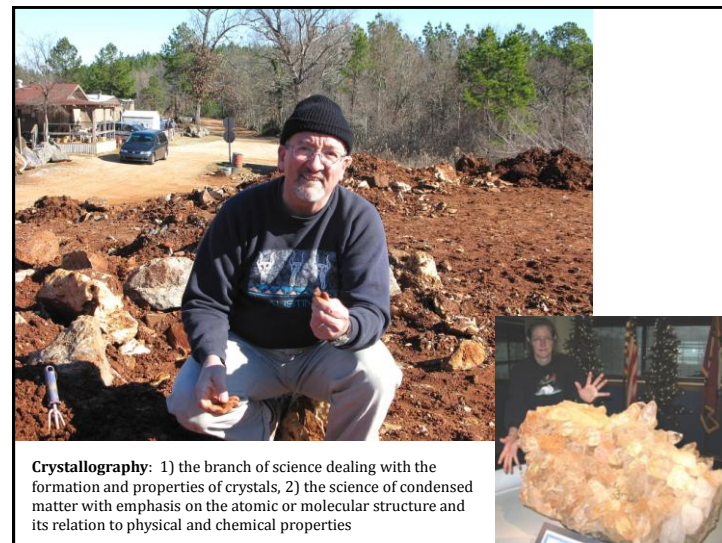


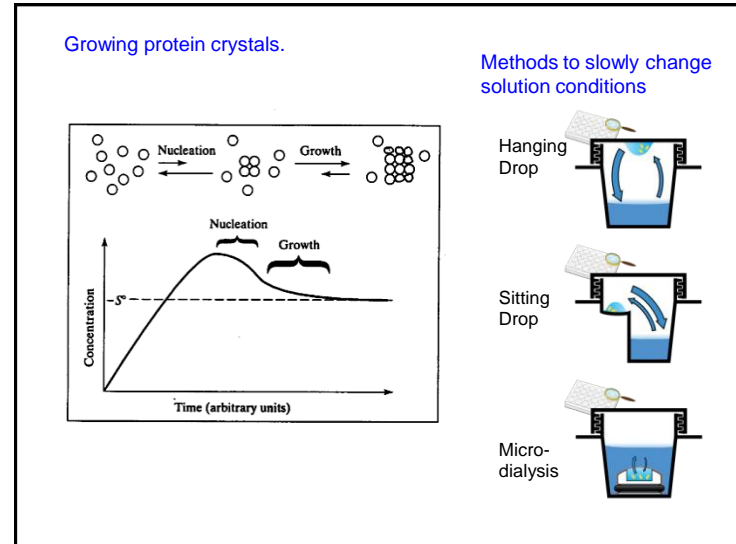
## Crystallography

2014  
International year of crystallography

Topics:

- Image Formation** (*what we see is not always accurate*)  
Resolution / Wavelength (Amplitude, Phase) / Diffraction & Interference  
Light Microscopy / EM / X-ray / (NMR)
- Protein Data Bank (PDB)**  
Data mining and Protein Structure Analysis Tools
- IYCr 2014 - Celebrating 100 years of X-ray Crystallography**
- X-Ray Crystallography – practical aspects**
  - ➔ a) Crystal Growth – Materials / Methods
  - ➔ c) Crystal Lattices - Lattice Constants / Space Groups / Asymmetric Unit
  - ➔ d) X-ray Sources – Sealed Tube / Rotation Anode / Synchrotron
  - e) Theory of Diffraction – Bragg's Law / Reciprocal Space
  - f) Data Collection – Methods / Detectors / Structure Factors
  - g) Structure Solution – Phase Problem: MIR / MR / MAD
  - h) Refinements and Models / Analysis and presentation of results





### Variables that influence crystal growth

1. **Nature of macromolecule** – Purity and concentration of macromolecule
2. **Nature and concentration of precipitant**
3. **pH / Temperature / Pressure**
4. Level of reducing agent or oxidant
5. Substrates, coenzymes, and ligands / Metal ions
6. Preparation and storage of macromolecule / Proteolysis and fragmentation
7. Age of macromolecule / Degree of denaturation
8. Vibration and sound
9. Volume of crystallization sample
10. Seeding
11. Amorphous precipitate
12. Buffers
13. Cleanliness
14. Organism or species from which the macromolecule was isolated
15. Gravity, gradients and convection

### Common Compounds used in Crystallization

**Ammonium sulfate** / or sodium

Sodium or ammonium citrate  
Sodium or ammonium acetate  
Magnesium sulfate  
Cetyltrimethyl ammonium salts

**Polyethylene glycol** 400, 1000, 2000, 4000, 6000, 8000, 15,000 M

### Methods for protein crystallization

Batch crystallization (simply dump reagents together)

Liquid-liquid diffusion in a capillary tube

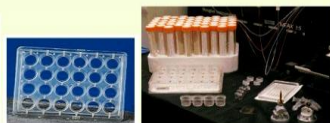
Vapor diffusion-the most successful method (**hanging drop**, **sitting drop**), typically using a Limbro plate. Equilibration occurs between the liquid and vapor phase.

Dialysis

## Hanging Drop Method - Crystal Screening

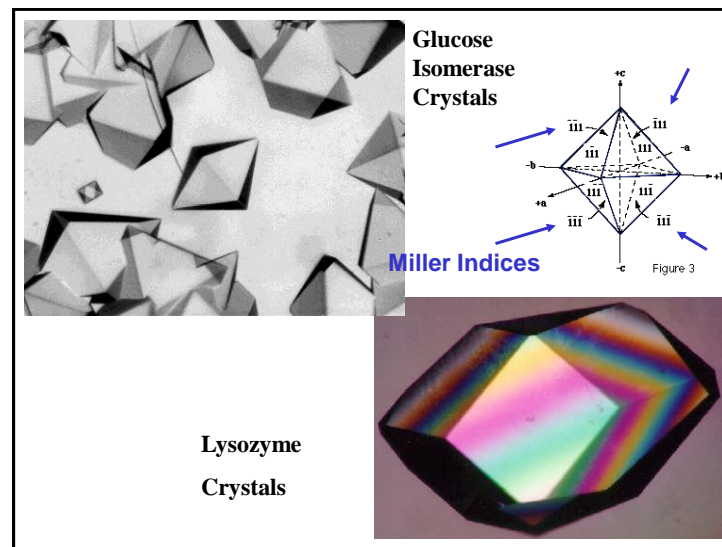
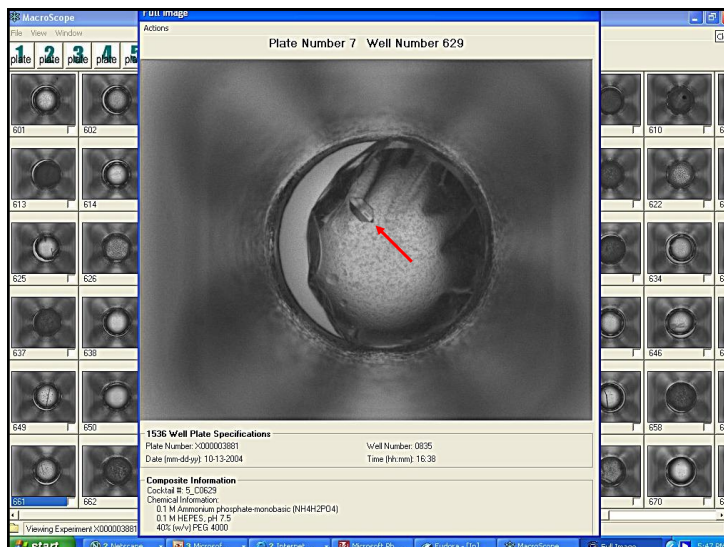
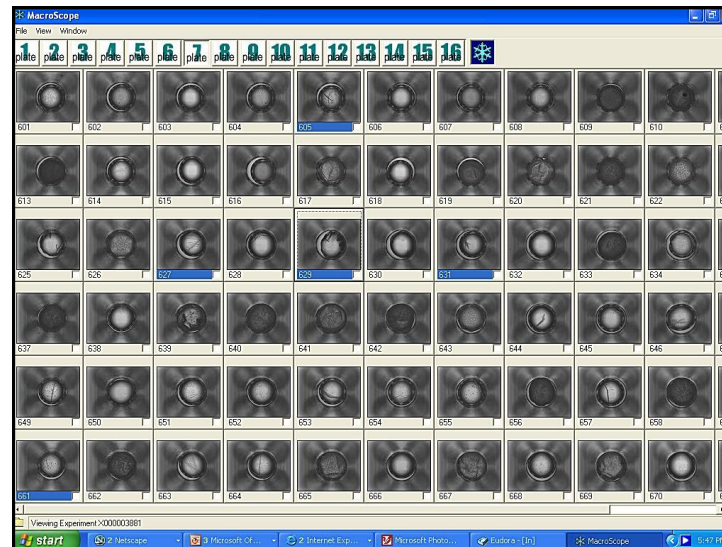
### The Experimental Setup

In order to obtain a crystal, the protein molecules must assemble into a periodic lattice. One starts with a solution of the protein with a fairly high concentration (2-30 mg/ml) and adds reagents that reduce the solubility close to spontaneous precipitation. By slow further concentration, and under conditions suitable for the formation of a few nucleation sites, small crystals may start to grow. Often very many conditions have to be tested to succeed. This is usually done by **initial screening**, followed by a systematic optimization of conditions. Crystals should be to a few tenth of a mm in each direction to be useful for diffraction experiments.



### Hampton Crystal Screen Solutions

Tube #	SALT	BUFFER	Precipitant	Miniscreen	Tube #
1	0.02M Calcium Chloride	0.1M Na Acetate pH 4.6	30% w/v 2-methyl-2,4-pentanediol	Y	1
2	None	None	0.4M K <sub>2</sub> Na Tartrate tetrahydrate		2
3	None	None	0.4M Ammonium dihydrogen phosphate		3
4	None	0.1M Tris-HCl pH 8.5	2.0M Ammonium Sulfate	Y	4
5	0.2M tri-sodium citrate	0.1M Na HEPES pH 7.5	30% w/v 2-methyl-2,4-pentanediol		5
6	0.2M Magnesium chloride	0.1M Tris-HCl pH 8.5	30% w/v PEG 4000		6
7	None	0.1M Na Cacodylate pH 6.5	1.4M Sodium acetate trihydrate		7
8	0.2M tri-sodium citrate	0.1M Na Cacodylate pH 6.5	30% w/v 2-propanol		8
9	0.2M Ammonium acetate	0.1M Na Citrate pH 5.6	30% w/v PEG 4000	Y	9
10	0.2M Ammonium acetate	0.1M Na Acetate pH 4.6	30% w/v PEG 4000	Y	10





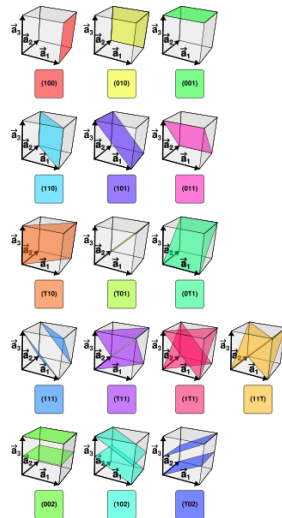
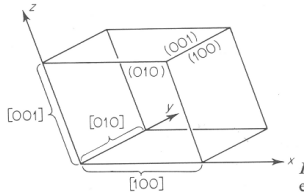
## Bragg Planes

X-ray scattering can be understood as if the x-rays are reflected from planes in the crystal.

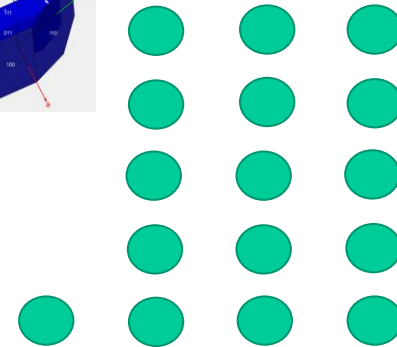
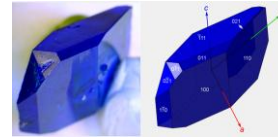
$h, k, l$  are integers, called "Miller indices"

Miller indices are used to define the direction of planes within a crystal. A plane with Miller indices  $h, k, l$  intersects the unit cell edges  $a, b, c$  at points  $a/h, b/k$  and  $c/l$ .

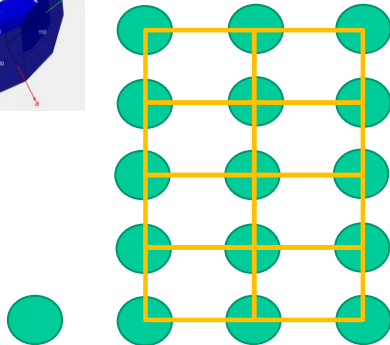
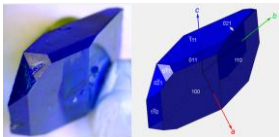
(3 integers define the direction of a plane).



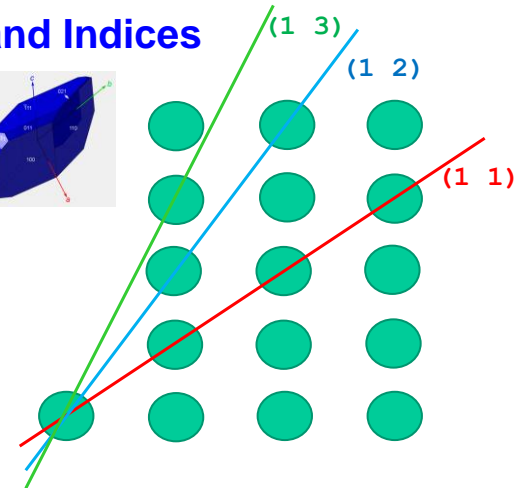
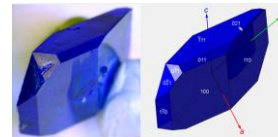
## Atoms in space

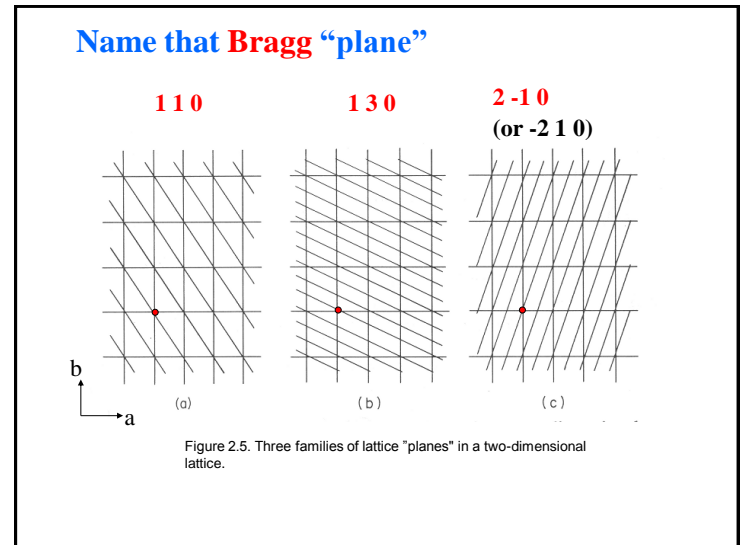
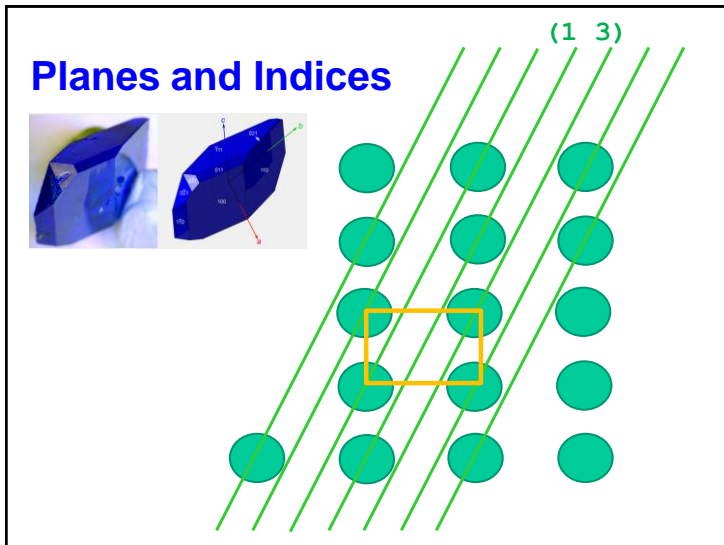
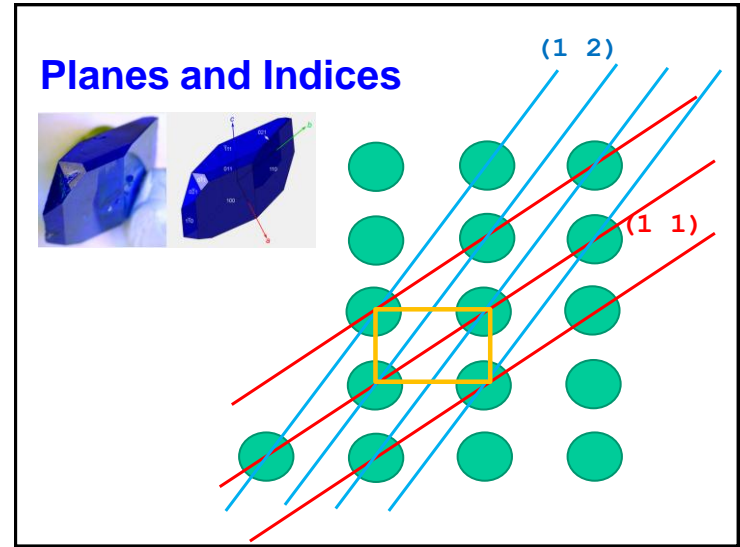
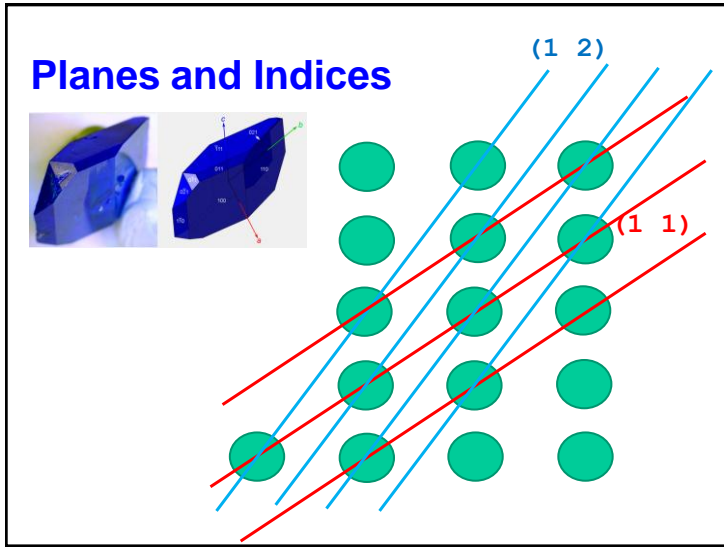


## Atoms in space / Unit Cell



## Planes and Indices





From Protein Molecule to Protein Crystal

