

### **History of NMR**

- First described by Isidor Rabi in 1938 when he was experimenting on lithium using molecular beams
- Felix Bloch and Edward Purcell expanded on Rabi's techniques in 1946, concentrating on NMR in liquids and solids





C. Moore, J. Bantseev, J. Miller & D. Lee - CH370 Student Presentation

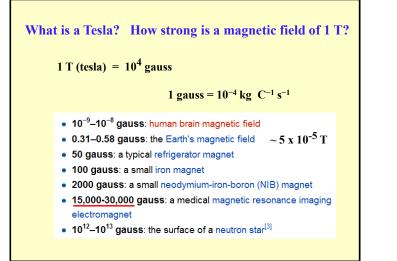
## What is NMR?

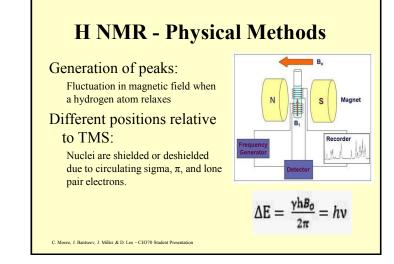
- An analytical chemistry technique used to determine content and purity of a sample, as well as the molecular structure
- Used to study known and unknown compounds
- Provides information about the number and types of atoms in a molecule

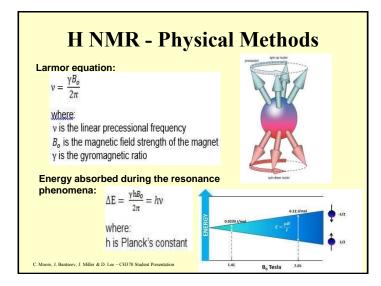


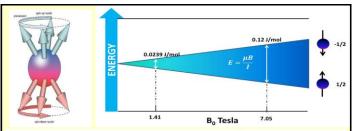


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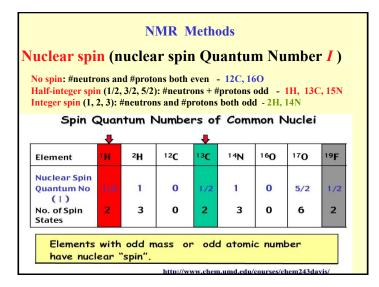


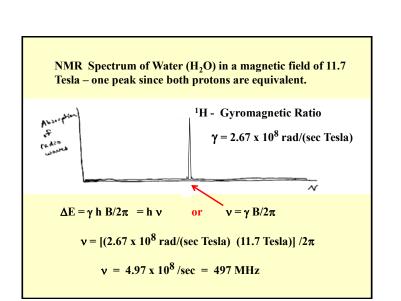
When a group of spins is placed in a magnetic field, each spin aligns in one of the two possible orientations either positive or negative. In sample, which contains a specific NMR-active nucleus, the nuclei will be distributed throughout the various spin states. The energy separation between these states is relatively small and the energy from thermal collisions is sufficient to place many nuclei into higher energy spin states. The number of nuclei in each spin state can be described by the Boltzmann distribution. The Boltzmann equation expresses the relationship between temperature and the related energy as shown below.

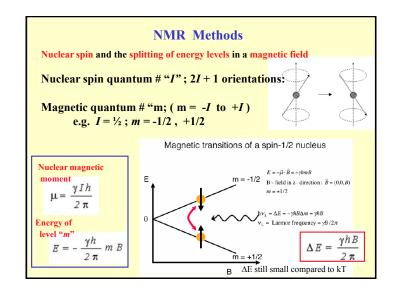
$$\frac{N_{upper}}{N_{lower}} = e^{\frac{-\Delta E}{kT}} = e^{\frac{-h\nu}{kT}}$$

Where N<sub>utper</sub> and N<sub>over</sub> represent the population of nuclei in upper and lowe energy states, E is the energy difference between the spin states, k is the Boltzmann constant (1.3805x10-23 J/Kelvin ) and T is the temperature in K. At room temperature, the number of spins in the lower energy level, N<sub>utper</sub>, slightly outnumbers the number in the upper level, N<sub>utper</sub>.

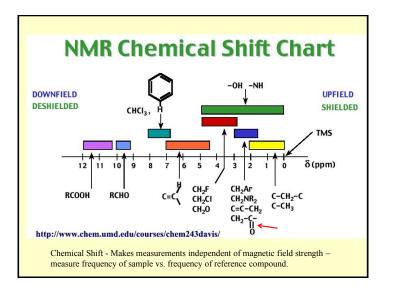
http://chemwiki.ucdavis.edu/Physical\_Chemistry/Spectroscopy/Magnetic\_Resonance\_Spectroscopies/Nuclear\_Magnetic\_Resonance/NMR%3A\_Theory#Distribution of Particles Between Magnetic Quantum States

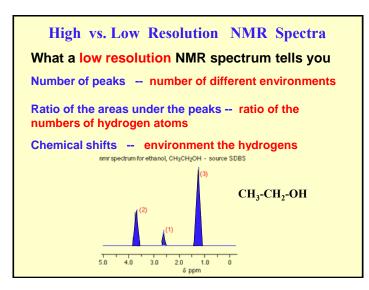


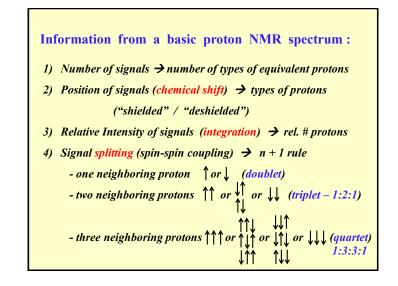


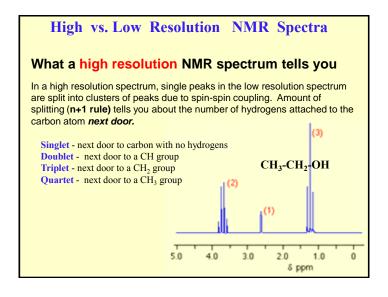


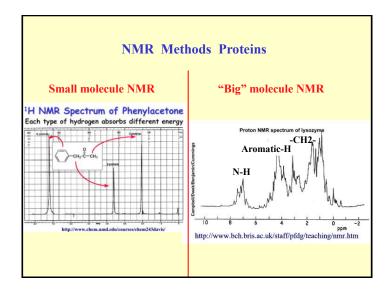
ΔE still small c	ompared to kT						
$\Delta E = \frac{\gamma h B}{2 \pi} = \mathbf{h} \mathbf{v}$	Boltzmann constant: $\mathbf{k} = \mathbf{R}/\mathbf{T}$ $PV = n\mathbf{R}T = N\mathbf{k}T$						
$\Delta E = h v \text{ with } v \sim 500 \text{ MHz}$ = 6.63 x 10 <sup>-34</sup> J-s (5.0x 10 <sup>8</sup> /s) = 3.31x 10 <sup>-25</sup> J	$kT = (1.38 \text{ x } 10^{-23} \text{ J/K})(298 \text{ K})$ = 4.11 x 10 <sup>-21</sup> J						
<b>Boltzmann distribution:</b> the probability of a system being in a state with energy E is proportional to $e^{-\Delta E / kT}$							
$\frac{n^+}{n^-} = e^{-\Delta E / kT} = exp(-3.31x \ 10^{-25} \ J/ \ 4.11 \ x \ 10^{-21} \ J$ $= exp(-0.00008) = 0.99992$							
for <b>100,992 nuclei</b>	$\frac{n^+}{n^-} = \frac{99,992}{100,000}$						

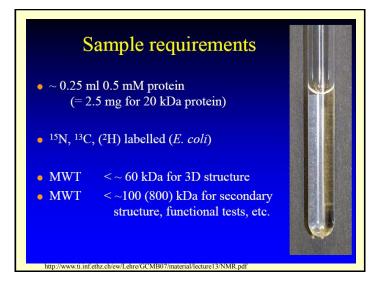








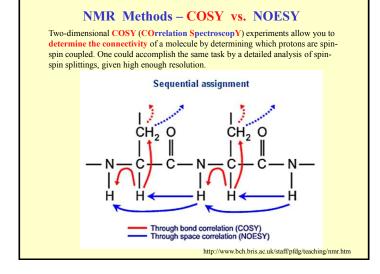




# Limitations for Structure Determination by Multidimensional NMR Methods Protein must be "smallish" (< 300-500 amino acid residues)</li> Protein must be soluble and well behaved in solution. (1-2 mM or 30 mg/mL for a 20kDa protein) Must be able to solve the "Assignment" Problem Gly43 CA-H vs. Gly87 N-H, etc. Must have sufficient number of distance restraints Gly43 CA-H / Gly87 N-H 3.0 – 4.5 A, etc.

# Structure Determination of Proteins in Solution

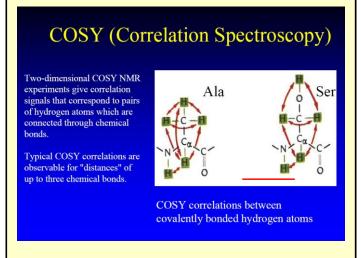
- Resonance assignment (COSY)
- Distance assignment (NOESY)
- Structure calculation

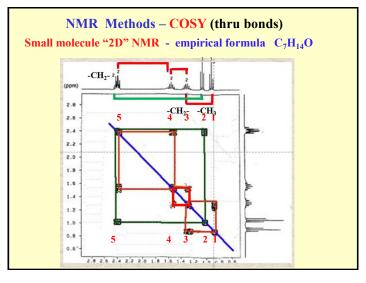


# Resonance assignment by COSY

- COSY spectra show frequency correlations between nuclei that are connected by chemical bonds
- Since the different amino acids have a different chemical structure they give rise to different patterns in COSY spectra
- This information can be used to determine the frequencies of all nuclei in the molecule. This process is called resonance assignment
- Modern assignment techniques also use information from COSY experiments with <sup>13</sup>C and <sup>15</sup>N nuclei

http://www.ti.inf.ethz.ch/ew/Lehre/GCMB07/material/lecture13/NMR.pdf





**NOESY** is a acronym for Nuclear Overhauser Effect Spectroscopy. NOE is the perturbation of the magnetization of one spin due to dipolar coupling with another spin. Since this interaction is detected through space the NOESY experiment provides important information on inter-nuclear distances.

 $\mathsf{NOE}$  = the change in the intensity of the NMR signal of one nucleus when the sample is irradiated with radiowaves at the NMR absorption frequency of another nearby nucleus.

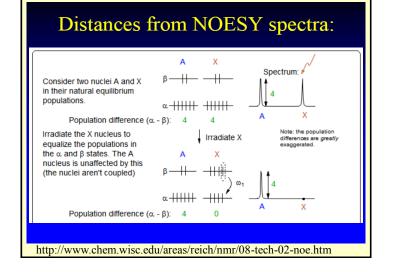
The NOE depends on the distance between nuclei.

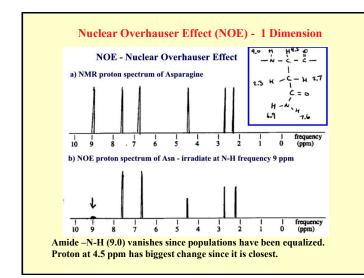
In general,

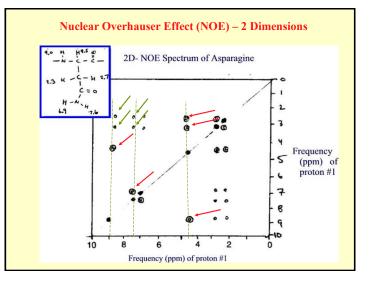
<sup>1</sup>H to <sup>1</sup>H distance = 3 Å there is a large NOE

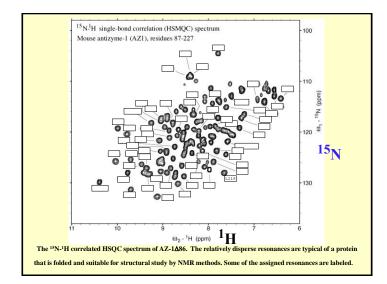
<sup>1</sup>H to <sup>1</sup>H distance = 4 Å there is a medium NOE

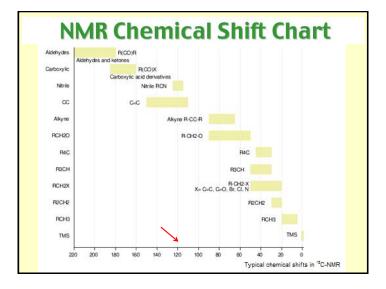
<sup>1</sup>H to <sup>1</sup>H distance =  $6 \text{ \AA}$  there is a small NOE





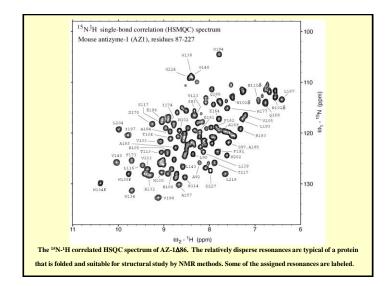


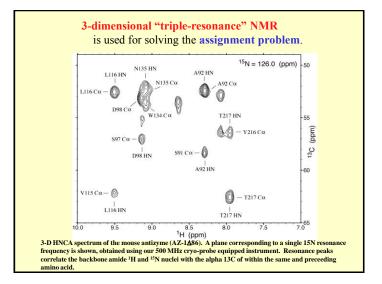


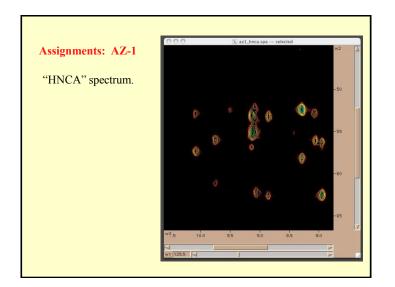


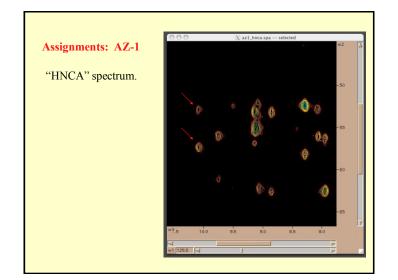
	NH		BH	Others
le sodiue	мн	an	рн	Others
ły		3.97		
la	8.25		1.39	
al	8.44	4.18	2.13	0.97,0.94(CH3)
•	8.20	423	1.90	21.48,1.10 (CHZ), 0.95 ( 7 CH3), 0.89 ( 8 CH3)
u	8.42	438	1.65,1.65	1.65 ( 7 CH), 0.94,0.90( 8 CH3)
10		4.44	2 28,2 02	2.03 ( 7 CH2), 3.68,3.65 ( 8 CH2)
ler .	8.38	4.50	3.88	
hr	8.24	435	422	1.23 ( 7 CH3)
sp	8.41	4.76	284,2.75	
bu	8.37	4.29	2.09,1.97	2.31,2.28 ( γ CHZ)
ys	8.41	436	1.85,1.76	1.45 ( ή CH2), 1.70 (δ CH2), 3.02 ( ε CH2), 7.53 ( ή NH2)
Arg		4.38	1 00 1 20	1.70 ( 7 CH2), 3.32 ( 6 CH2), 7.17,6,62 (NH)
<sup>rg</sup>	0.41	•.30	1.69,1.79	1.50( 7 cm2), 3.52 ( 0 cm2), 7.17,6,62 (m)
l ans	8.75	4.75	2.83,2.75	7.59,6.91 ( <b>ð</b> NH2)
7In	8.41	4.73	2.13,2.01	2.38 ( 7 CH2), 6.87,7.59 ( 7 NH2)
det	8.42	4.52	215201	2.64( ↑ CH2), 2.13 ( € CH3)
ys.			3.28,2.96	
P	and an			7.1-7.5 (aromatic), 10.22 (NH)
he	-			7.3-7.4 (aromatic)
η a				6.83-7.15 (aromatic)
	8.41	4.63	3.26,3.20	7.14-8.12 (aromatic)

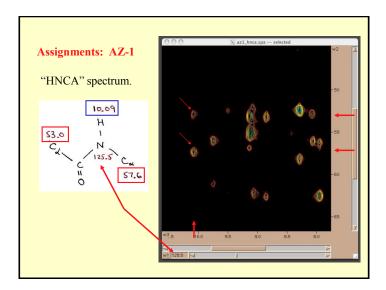
۲	0	0					az1_		36.xls				
0	A	B	С	D	E	F	G	H	I	J	K	L	М
1	no		HN	N	CA	CA-1	CB	CB-1	CO	CO-1	HA	HB	HG
2	87	D											
3	88	H											
4	89	S			58.6		63.7		173.9		4.42		
5	90	L	8.42	124.2	55.2		42.3		176.7				1.82,1.57
6	91	S	8.24	116.1	58.1	55.1	63.8		173.3			3.92	
7	92	A	8.27	125.6	52.4		19.4		176.6				
8	93	S	8.39	115.2	57.8		64.2		172.8				
9	94	I	8.62	124.3	61.1		37.6		175.0				
10	95	L	8.70	130.2	55.9		43.9		175.9				
11	96	Y	7.82	119.1	58.1		42.5		171.9				
12	97	S	7.62	121.6	57.0		65.3					3.77,3.66	
13	98	D	9.14	126.0	53.1	57.0	40.8		174.8				
14	99	E	8.76	115.8	59.1							2.33,2.06	
15	100	R	8.82	118.1	56.8	59.0	32.4		174.8				
16	101	L	8.60	121.5	53.9	56.4	46.7	32.6	174.3	174.8	5.32	1.66,1.60	1.26
17	102	N	8.70	119.6	53.7	53.9	42.0	46.5	173.5	174.2	5.20	2.75	
18	103	V	9.41	127.0	61.3	53.8	33.4	42.0	174.2	173.5	5.11	2.05	
19	104	т	8.89	121.1	60.0	61.3	71.4	33.4	172.0	174.2	5.13		1.17
20	105	E	8.96	123.7	55.0	60.0	31.9	71.6	175.2	172.2	5.21		
21	106	E	8.87	127.1	54.0	55.0	29.7	32.0		175.4	4.78	1.85	
22	107	P	no		56.8		32.3						
23	108	T	7.94	114.4		56.8		32.5	172.3	176.0	4 66	4.04	1.12
24	109	S	8.59	123.8		61.6		70.9		172.5			
25	110	N			53.1		39.3						
26	111	D	8.47	119.8	55.1	53.0		39.3		173.9	4.51	2.76	
27	112	ĸ			56.9		28.6		173.5		5.19		
28	113	T	9.09	123.6		56.9	69.1	28.6	173.3	173.5			1.16
29	114	R	8.58	128.8	55.1			69.1				1.68, 1.80	
30	115	Y	9.05	125.2		54.8	33.2		174.0				1.03,0.98
31	116	L	9.50	126.4					175.3				2.15,0.96
32	117	S	9.08	117.8	57.1		63.1					3.85, 3.72	
33	118	I	9.38	128.0		57.1	39.3	63.1		173.7			
34	119	Q	8.95	127.9								1.95, 2.12	

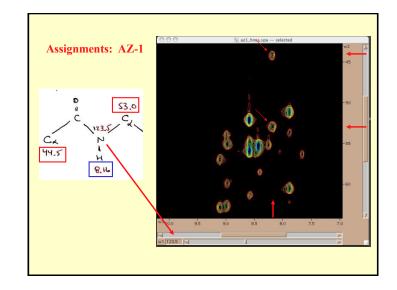


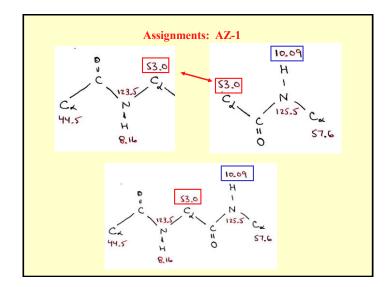


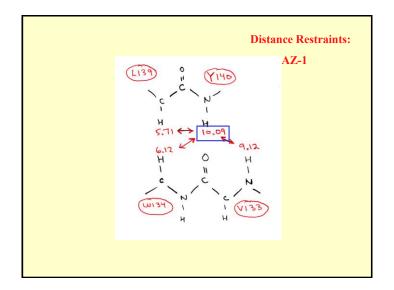


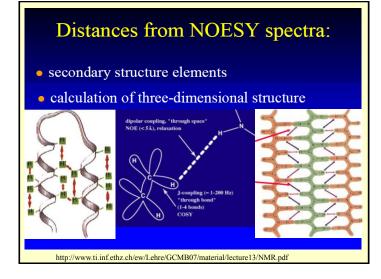










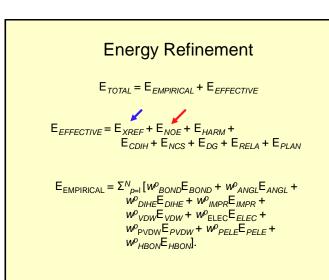


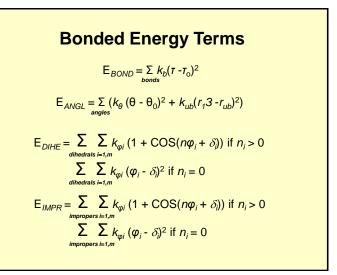
#### Types of restraints available from NMR experiments

- 1. NOEs give rough distances between assigned atoms given as upper and lower bounds.
- 2. COSY spectra and J-couplings give dihedral angle restraints

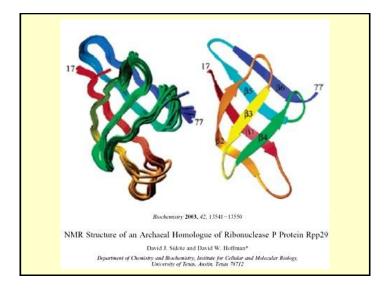
Also have constraints from what you know about the protein:

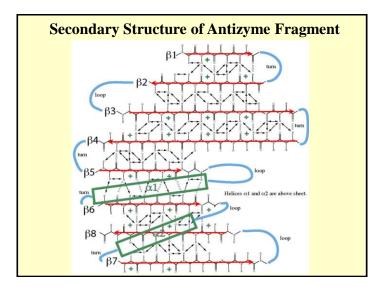
- 1. Connectivity due to known aa geometry & sequence
- 2. Standard bond lengths and angles

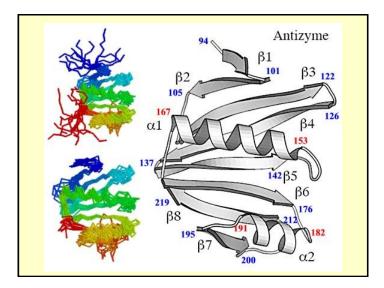


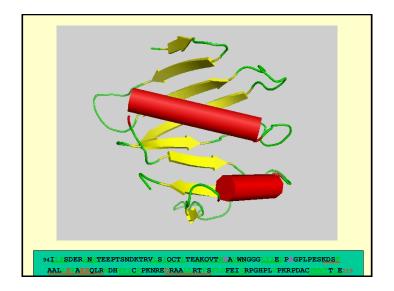


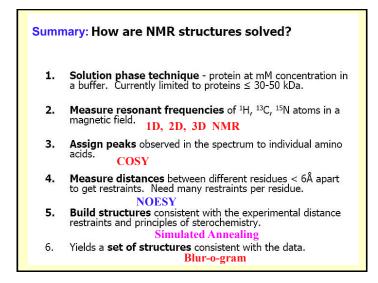
intraresidue NOEs	215
sequential NOEs (residue $i$ to $i + 1$ )	178
medium-range NOEs (residue <i>i</i> to $i + 2, 3, 4$ )	18
long-range NOEs	143
dihederal angle restraints	70
hydrogen bond restraints	27
total structural restraints	651
no. of unique starting structures for simulated annealing	10
no. of simulated annealing runs, differing in initial trajectories	200
rmsd for backbone atoms (residues 17-77)	0.87 Å
rmsd for side chain atoms (residues 17-77)	1.78 Å
av no. of NOE violations > 0.2 Å (per structure)	$3.2 \pm 1.0$
av no. of NOE violations > 0.5 Å	0
(per structure)	
residues in most favored regions of	$71.2 \pm 2.6\%$
the Ramachandran plot	
residues in additionally allowed regions of	$21.2 \pm 4.6\%$
the Ramachandran plot	a the showing the
residues in generously allowed regions of	$5.8 \pm 2.7\%$
the Ramachandran plot	2.0 + 2.779
residues in disallowed regions of	$1.9 \pm 0.9\%$
the Ramachandran plot	
rmsd for covalent bonds	$0.0034 \pm 0.000$
rmsd for covalent angles	$0.511 \pm 0.015$
rmsd for improper angles	$0.581 \pm 0.016$

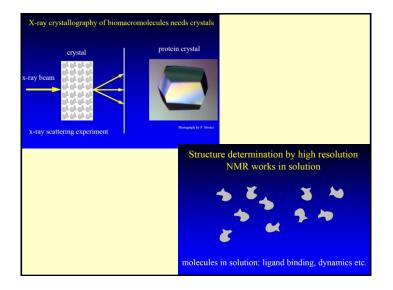












### Comparison of X-ray vs. NMR Structure Determination

a) Limitations.

X-ray: Need crystals NMR: MW limit (over about 40 kDa spectra are too complex to interpret)

b) Ease of structure determination.

c) Quality of structural information obtained.

X-ray: Usually has the advantage, especially with high-resolution structures, due to direct visualization of the molecule.

NMR: Very good quality structures are also obtained, though usually not as detailed as the best x-ray structures. Quality of the NMR structure depends on the # of distance and angle constraints obtainable from the data.

d) NMR has some advantages over x-ray crystallography:

Information may be obtained on the dynamics of structures. Such as hydrogen bond opening frequencies, & rotational times of bond vectors.