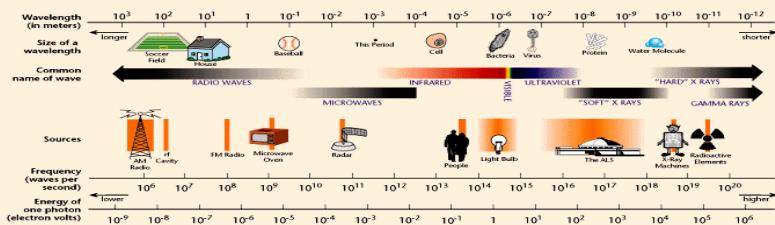
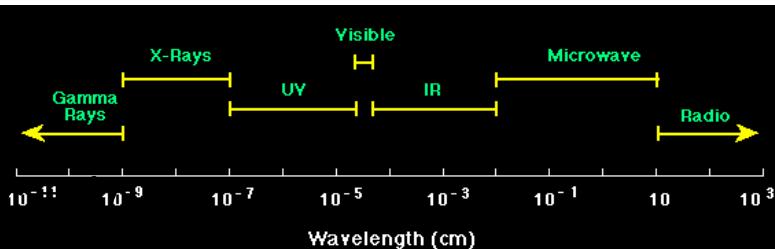
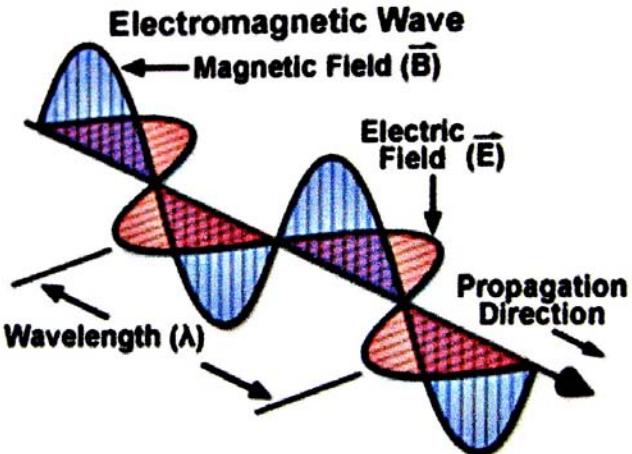


# Spectroscopy

## THE ELECTROMAGNETIC SPECTRUM



- Objectives:** Review nature of electromagnetic radiation ( $\lambda / \nu / c$ )  
 Interactions of "Light" with matter (Absorption / Scattering)  
 Frank-Condon Principle  
 Electronic transitions  
 Beer Lambert Law ( $A = O.D. = -\log(T) = \epsilon \cdot [c] \cdot l$ )  
 Excitation Transfer / FRET



$$\text{Speed of light } (\nu) = \text{wavelength } (\lambda) \times \text{frequency } (\bar{\nu})$$

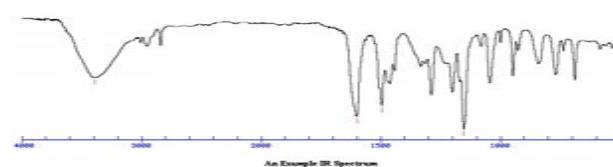
**Wavenumber**,  $\bar{\nu} = \frac{1}{\lambda}$ , is the number of wave maxima per cm.

Units are  $\text{cm}^{-1}$ . 700 nm **red light** =  $1.43 \times 10^4 \text{ cm}^{-1}$   
 420 nm **violet light** =  $2.38 \times 10^4 \text{ cm}^{-1}$

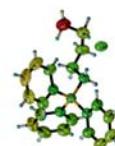
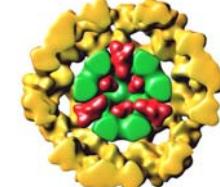
Velocity of light changes in different substances.

**Index of refraction** of a substance,  $n = c / v$

## Light and Matter: Absorption (spectroscopy) Scattering (image formation)

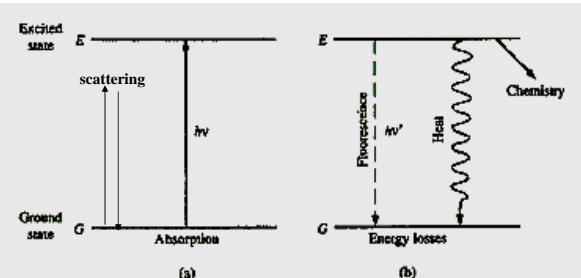


- Light Photography  $\lambda \sim 400 - 700 \text{ nm}$
- Electron Microscopy  $\lambda \sim 0.001 - 0.1 \text{ nm}$
- X-Ray or NMR  $\lambda \sim 0.1 \text{ nm}$



When light interacts with matter, there are **two possibilities**:

1. **Scattering** - the light is transmitted but velocity changes.
2. **Absorption** (photons are absorbed)
  - a. they produce heat
  - b. they cause a chemical change
  - c. they are reemitted (fluorescence, phosphorescence)



The oscillating electric field induces a force on the charged particles (electrons, protons).

If the **frequency of oscillation corresponds to an energy-level difference**, the photon will be **absorbed** - its energy will change form into electron or nuclear motion.



Time frame for **absorption**:

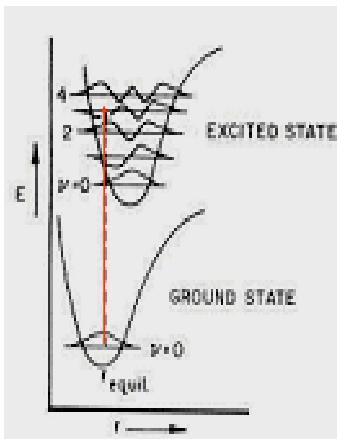
The **absorption usually occurs in the time it takes one wavelength to pass the molecule**.

the speed of light,  $c = 3 \times 10^{17} \text{ nm sec}^{-1}$   
for uv light, the wavelength,  $\lambda \approx 300 \text{ nm}$ .

$$3 \times 10^2 \text{ nm sec} / 3 \times 10^{17} \text{ nm} = 10^{-15} \text{ sec}$$

## Frank-Condon Principle

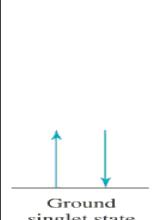
- "The **nuclear motion** ( $10^{-13} \text{ s}$ ) is much slower as compared with **electronic motion in transition** ( $10^{-15} \text{ s}$ ), so it is negligible during the time required for an electronic excitation."
- Since the nucleus does not move during the excitation, the internuclear distance keeps the same, and "the most probable component of a electronic transition involves only the **vertical transitions**".



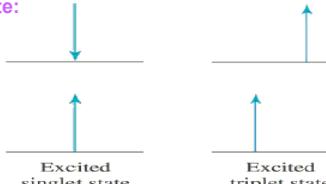
## Electronic transitions

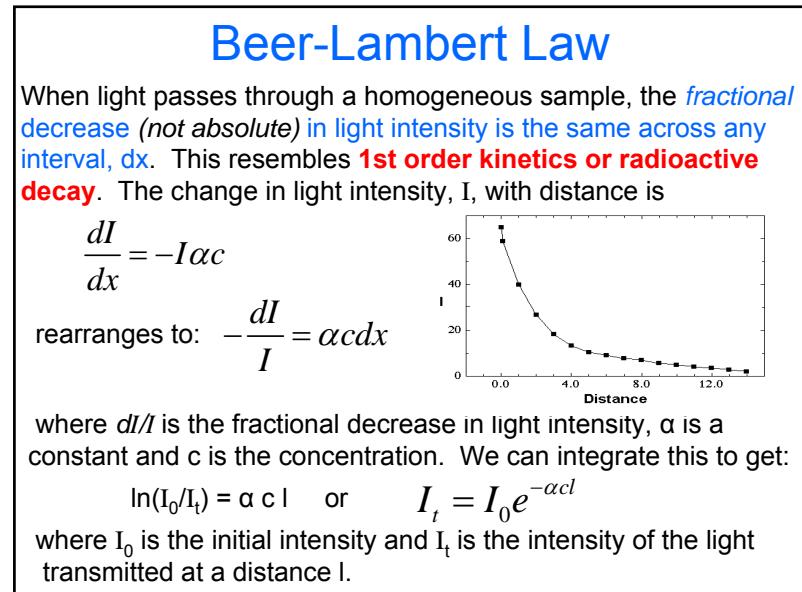
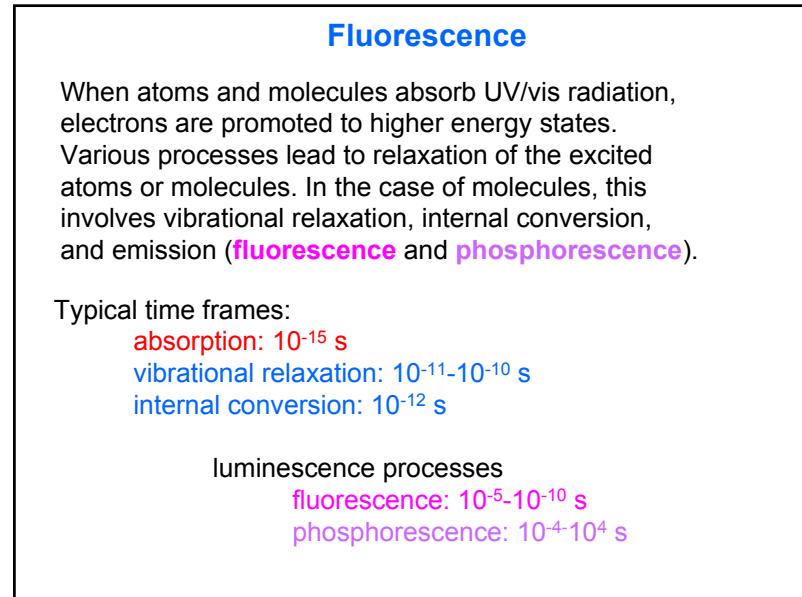
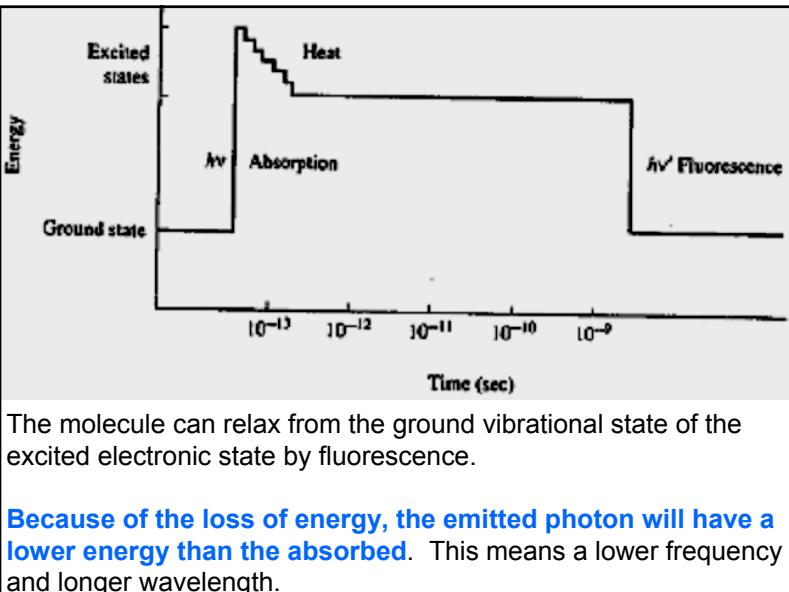
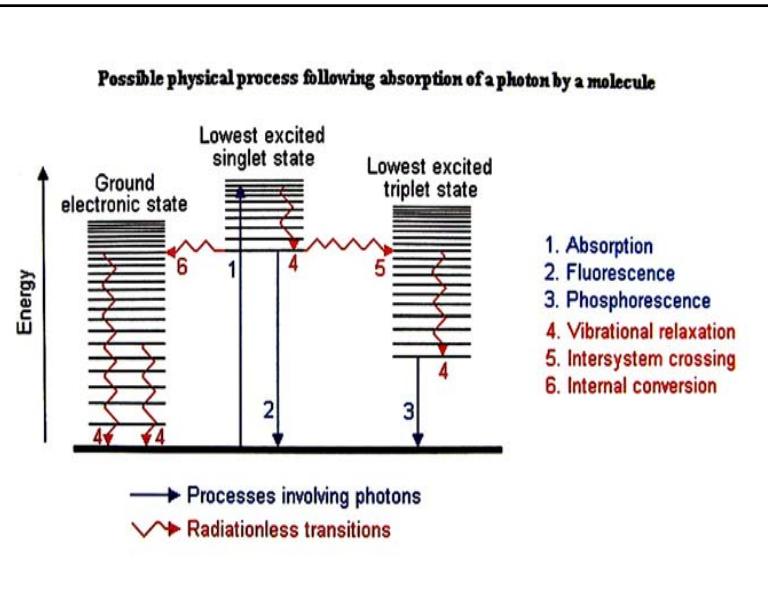
- **Selection rules:** allow  $S \rightarrow S$ , and  $T \rightarrow T$  processes but **not**  $S \rightarrow T$  and  $T \rightarrow S$ . Ground states are usually singlets; thus **most excitations are to singlet excited states**, like  $S_0 \rightarrow S_1$ ,  $S_0 \rightarrow S_2$ , ...
- **Triplet states are usually formed by intersystem crossing** from an excited singlet state, such as  $S_1$ , rather than by direct excitation from the  $S_0$  ground state.

Fluorescence - from an **excited singlet state**



Phosphorescence - from an **excited triplet state**





It follows that the **transmitted intensity decreases exponentially with concentration**.

$$A = \log \frac{I_0}{I_t} = \epsilon cl$$

Units on  $\epsilon$ : M<sup>-1</sup> cm<sup>-1</sup>

where **A** is "absorbance" or "optical density" and  $\epsilon$  is the "molar absorptivity" or "molar extinction coefficient" and  $\epsilon = \alpha / 2.303$

#### Absorption Spectrum – "fingerprint"

Beer-Lambert Law: Intensity ( $I$ ,  $I_0$ ); Transmittance ( $T = I / I_0$ )

$$\text{Absorbance (A)}: A = \log (I_0 / I) = \log (1/T)$$

Extinction Coefficient – E (1%),  $\epsilon_M$  = Molar extinction coeff.  
 $A = O.D. = \epsilon \cdot c \cdot l$  also [  $E(1\%) \cdot MW = 10 \cdot \epsilon_M$  ]

Proteins: A280 ; E (1%) ~ 10 (or O.D. of 1 for 1 mg/mL)

Nucleic Acids: A260 ; E (1%) ~ 200 (or O.D. of 1 for 50 mg/mL)

#### Environmental Effects

$I_{\text{nonpolar}} > I_{\text{polar}}$  (folding / unfolding effect)

DNA – Helix-Coil Transitions ( $\epsilon_{\text{free base}} > \epsilon_{\text{ss}} > \epsilon_{\text{ds}}$ ) follow denaturation

## Excitation Transfer

Fluorescence Resonance Energy Transfer (FRET) is an important tool for studying macromolecular structure and dynamics in solution. Some amino acids fluoresce and the **energy transfer strongly depends on distance between donor and acceptor** making it a valuable tool to study protein **folding** and other **dynamics**.

Consider an excited donor,  $D^*$  and an acceptor that can be excited to a fluorescent state,  $A^*$ .

$D \rightarrow D^*$  (absorption of light,  $h\nu$ , by donor)

$D^* \rightarrow D + h\nu'$  (donor fluorescence)

$D^* + A \rightarrow D + A^*$  (excitation transfer)

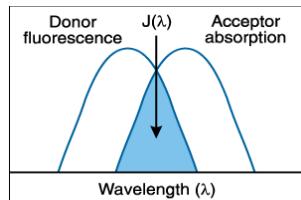
$D^* \rightarrow D$  (other deexcitation)

$A^* \rightarrow A + h\nu''$  (acceptor fluorescence)

#### Primary Conditions for FRET

- Donor and acceptor molecules must be close (~10–100 Å).
- Absorption spectrum of acceptor must overlap the fluorescence emission spectrum of the donor.
- Donor and acceptor transition dipoles must be ~ parallel.

FRET spectral overlap.



#### Experimental Measurements

1. **Decrease in fluorescence quantum yield** of donor in the presence of acceptor.
2. **Decrease in fluorescence lifetime of acceptor** in the presence of donor.
3. **Increase in the fluorescence of D** in the presence of A.

#### Förster Radius, $R_o$

The distance at which energy transfer is 50% efficient is defined by the Förster radius ( $R_o$ ). The magnitude of  $R_o$  is dependent on the spectral properties of the donor and acceptor dyes and the **efficiency depends on the inverse sixth power of intermolecular distance**:

$$\text{Efficiency} = k_T / (k_T + k_d) = r_0^6 / (r_0^6 + r^6)$$

where  $k_d$  is the rate constant for de-excitation, and  $k_T$  is the rate constant for transfer.

$$R_o = [8.8 \times 10^{23} \cdot \kappa^2 \cdot n^{-4} \cdot \phi_d \cdot J(\lambda)]^{1/6} \text{ Å}$$

where  $\kappa^2$  = dipole orientation factor (range 0 to 4;  $\kappa^2 = 2/3$  for randomly oriented donors and acceptors)

$\phi_d$  = fluorescence quantum yield of the donor in the absence of the acceptor

$n$  = refractive index of the medium

$$J(\lambda) = \text{spectral overlap integral} = \int \epsilon_A(\lambda) \cdot F_D(\lambda) \cdot \lambda^4 d\lambda \text{ cm}^3 \text{M}^{-1}$$

where  $\epsilon_A$  = extinction coefficient of acceptor

$F_D$  = fluorescence emission intensity of donor as a fraction of the total integrated intensity