# **Centrifugation - Goals for this unit:**

- 1. Understand essential theoretical concepts of movement of a particle under a centrifugal force.  $F_s + F_h + F_f = 0$
- 2. Know differences between "preparative" and "analytical" types of centrifugation. RCF = Relative Centrifugal Force
- 3. Analytical Centrifugation

Instrument

Optic systems - generalprinciples / how to interpret them

Schlieren / Interference / Absorption optics

Common Applications (transport vs. equilibrium experiments)

Sedimentation Coefficient - "s" vs. "S"

Diffusion Coefficient D = RT/Nf

Frictional Coefficient / frictional coeff. ratio  $f = 6\pi\eta R$ 

Sedimentation Equilibrium

### Table 1. Approximate Values of Partial Specific Volumes for Common Biological Macromolecules

Substance	⊽ (mL/g)		
Proteins	0.73	(0.70-0.75)	
Polysaccharides	0.61	(0.59-0.65)	
RNA	0.53	(0.47-0.55)	
DNA	0.58	(0.55-0.59)	

Data from Beckman review article by Greg Ralston

#### **Sedimentation of Particles in a Gravitational Field**

constant velocity = 
$$u$$

$$m$$

$$F_{\rm f} = -fu$$

$$m$$

$$F_{\rm b} = -m_0\omega^2 r$$

$$F_{\rm s} = m\omega^2 r = \frac{M}{N}\omega^2 r$$

$$F_{\rm s} + F_{\rm b} + F_{\rm f} = 0$$

$$\frac{M}{N}\omega^2 r - \frac{M}{N}\bar{v}\rho\omega^2 r - fu = 0$$

$$\frac{M}{N}(1 - \bar{v}\rho)\omega^2 r - fu = 0$$

$$\frac{M}{N}(1 - \bar{v}\rho)\omega^2 r - fu = 0$$

## **Preparative Centrifugation**

1. Principles of Centrifugation / theory and key equations

$$F_{\rm S} = m\omega^2 r = \frac{M}{N}\omega^2 r$$

where  $\omega = \text{angular velocity (radians / sec)}$ 

r = radius of particle from axis of rotation

note:  $\omega$  (1/sec) = rpm x (2 $\pi$  rad / rev) x (1 min / 60 sec)

RCF (Rel. Centrifugal Force) = 
$$\frac{Fc}{Fg} = \frac{m\omega^2 r}{ma} = \frac{(2\pi \text{ rpm/60})^2 \text{ x r}}{980 \text{ cm/sec}^2}$$
  
= 1.119 x 10<sup>-5</sup> (rpm)<sup>2</sup> r

for 
$$r = 9.0 \text{ cm}$$

rpm	1000	5000	10,000	20,000	40,000
RCF	100	2500	10,000	40,000	160,000

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# **Use of Centrifugation in Biochemistry**

$$\frac{M(1-\bar{v}\rho)}{Nf} = \frac{u}{\omega^2 r} \equiv s$$

- 1. Preparative Centrifugation
  - rotors
  - density gradient methods

sucrose gradients / isopyncic methods (CsCl gradients)

- 2. Analytical Ultracentrifugation
  - instrument and optic systems
  - **sedimentation velocity** experiments

sed. coefficient (s)  $(S = 10^{-13}s)$ 

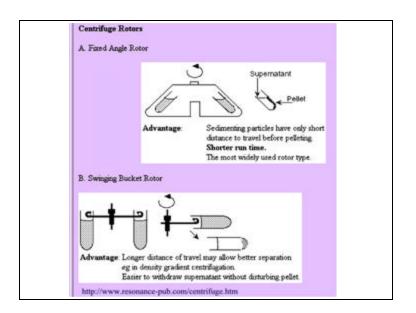
- sedimentation equilibrium exp.

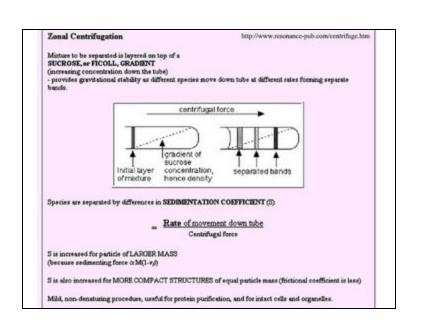
molecular weight

- diffusion constants /

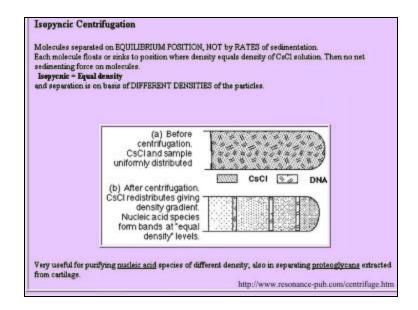
$$D = \frac{RT}{Nf}$$

# In sheence of a density gradient, separated bands of solute in the centerfuge are gravitationally unstable. Solute band Solvent Solvent Focating tube CANT OCCUR because layer of concentrated, dense solution overlaying less dense solvent would lead to mixing by convection and multip'the separation. In sheence of stebulang density gradient, can form households (of electrophoreau 9.3) but not some. In analytical ultracentrising, moving bounduries and concentration distributions observed by optical device. Create DENSITY GRADENT in table Use a non-interacting, low M. Wi solute in continuously interesting concentration from meniorus to bottom of tube. Important technique for pushing proteins and particularly markets acids. Twe different types of density gradient centralinguism, for two different pusposes are: - Zonal (or Rate Zonal) Centrifugation (Sucross density gradient centralinguism) - Important chloride density gradient centralinguism)





2.



#### **Molecular Weight Determination**

Light scattering / Centrifugation / Osmometry/ X-ray diffraction / Mass Spec

Electrophoresis and chromatographic methods are popular for rapid estimation of molecular weights of proteins and nucleic acids. However, such methods, though rapid and sensitive, have no rigorous theoretical base; they are empirical techniques that require calibration and assumptions that may be invalid.

The analytical ultracentrifuge enables the direct measurement of molecular weights of solutes in the native state and as they exist in solution, without calibrations or assumptions concerning shape. The method is applicable to molecules with molecular weights ranging from several hundreds (sucrose) up to many millions (virus particles).

Sedimentation equilibrium methods require only small sample sizes (20-120  $\mu$ L) and low concentrations (0.01-1 g/L).

# **Analytical Ultracentrifuge:**

# The sorts of questions for which answers are sought

- (1) Is the sample homogeneous? Is it pure?
- (2) If there is a single component, what is the molecular weight?
- (3) If more than one type present, can the molecular weight distribution of the sample be obtained?
- (4) Can an estimate be obtained of the size and shape of the particles? Are the molecules compact and spherical (globular) or long and thin (rodlike)?
- (5) Can the macromolecules be distinguished on the basis of density?
- (6) Can interactions between solute molecules be detected? Aggregation between molecules changes molecular weight, changes in molecular weight as a function of the concentrations of the components can illuminate the type of reaction (e.g., reversible or nonreversible?), the stoichiometry, and the strength of binding.
- (7) Can changes in conformation or shape of the particles be measured?

# **Conformational Changes**

X-ray diffraction and NMR techniques are currently the only techniques available that are capable of providing structural details at atomic resolution.

Nevertheless, the overall size and shape of a macromolecule or complex in solution can be obtained through measurement of the rate of movement of the particles through the solution. Sedimentation velocity experiments in the analytical ultracentrifuge provide sedimentation and diffusion coefficients that contain information concerning the size and shape of macromolecules and the interactions between them. Sedimentation coefficients are particularly useful for monitoring changes in conformation in proteins.

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# **Use of Centrifugation in Biochemistry**

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- 1. Preparative Centrifugation
  - rotors
  - density gradient methods

sucrose gradients / isopyncic methods (CsCl gradients)

- 2. Analytical Ultracentrifugation
  - instrument and optic systems
  - **sedimentation velocity** experiments sed. coefficient (s)  $(S = 10^{-13}s)$
  - **sedimentation equilibrium** exp. molecular weight
  - diffusion constants /

# **Centrifugation: Terms and Units**

Force: mass x acceleration (F = ma =  $mwr^2$ )

 $(g cm / sec^2)$ 

Energy: force x distance Joule =  $Kg m^2 / sec^2$ 

 $erg = g cm^{2} sec^{2}$ 

Partial specific volume  $\bar{v}$  (cm  $^3/g$ )

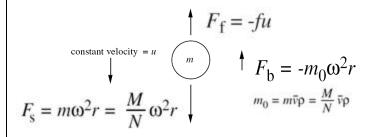
Viscosity: **h** (~0.01 g /(cm-sec))

Frictional Coefficient:  $f = 6 p h R_0 (\sim 10^{-8} \text{ g/sec})$ 

Sedimentation Coefficient:  $s (sec) [1S = 10^{-13} s]$ 

Diffusion Constant:  $D = \frac{RT}{Nf}$  (cm<sup>2</sup>/s)

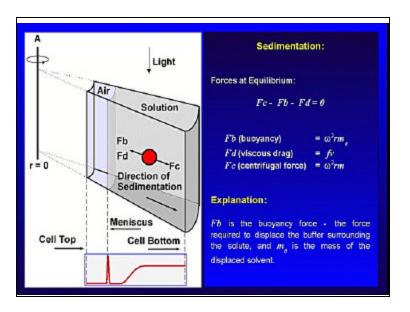
### **Sedimentation of Particles in a Gravitational Field**

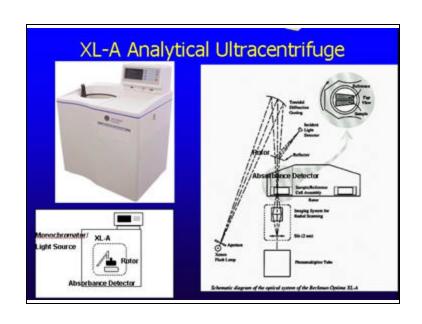


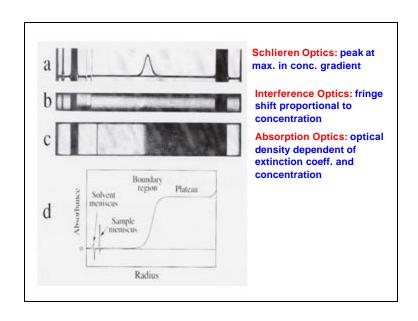
$$\frac{M(1 - \bar{\nu}\rho)}{Nf} = \frac{u}{\omega^2 r} \equiv s$$

$$D = \frac{RT}{Nf}$$

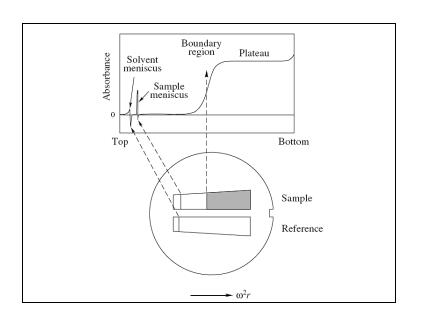
$$M = \frac{s^0 RT}{D^0 (1 - \bar{v}\rho)}$$

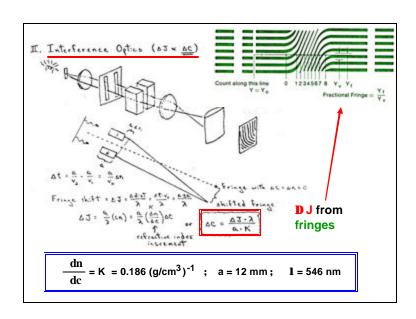


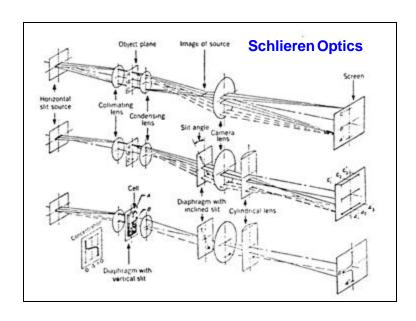


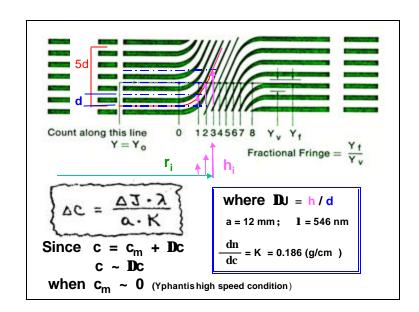


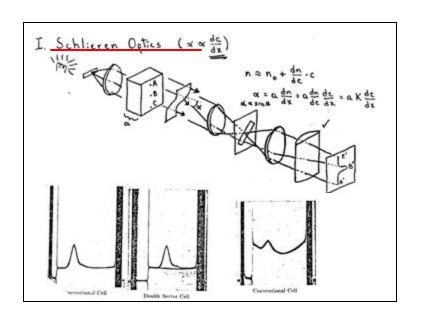


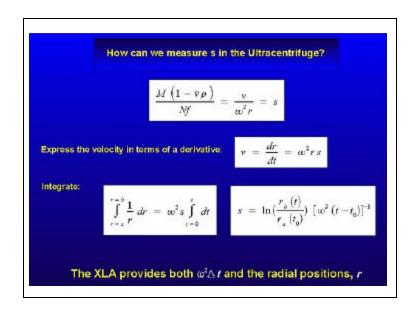




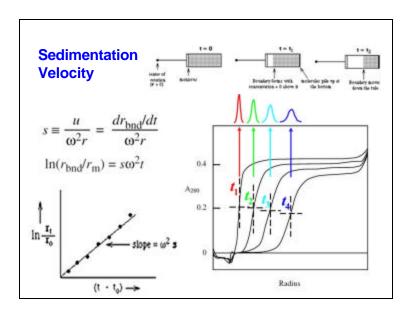


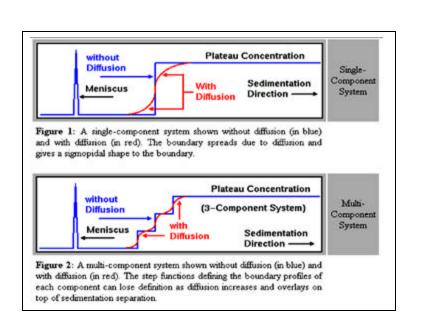


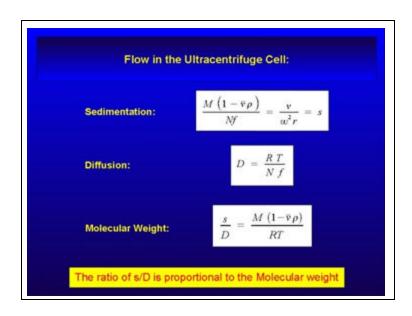




$$s \equiv \frac{u}{\omega^2 r} = \frac{dr_{\rm bnd}/dt}{\omega^2 r}$$
 
$$\ln(r_{\rm bnd}/r_{\rm m}) = s\omega^2 t$$
 Recall: 
$$s = \frac{v}{\omega^2 r} = \frac{1}{\omega^2} \frac{1}{r} \frac{d}{dt} \text{ This is a } \underbrace{\text{Differential Equation}}_{t_0} \text{ which we can easily solve by}$$
 separating the variables and integrating: 
$$\int_0^t \omega^2 s \, dt = \int_{t_0}^1 dr \quad \Longrightarrow \quad \omega^2 s(t \cdot t_0) = \ln \frac{r_t}{r_0}$$
 We integrate between  $t = t_0$  ( $r = r_0$ ) and  $t = t$  ( $r = r_0$ ); so the boundary position at the start ( $t = t_0$ ) and  $r_t$  is the boundary position at later time(s). Thus, if we plot 
$$\ln \frac{r_t}{r_0} \text{ vs. } (t \cdot t_0), \text{ the result is a straight line with a slope} = \omega^2 s.$$
 
$$s_{20,w} = s_{\text{obs}} \left( \frac{\eta_{T,w}}{\eta_{20,w}} \right) \left( \frac{\eta_s}{\eta_w} \right) \left( \frac{1 - \bar{v} \rho_{20,w}}{1 - \bar{v} \rho_{T,w}} \right)$$







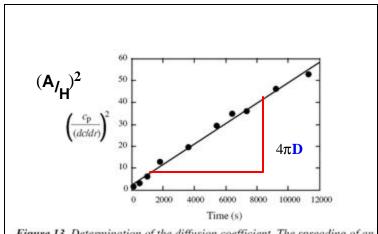
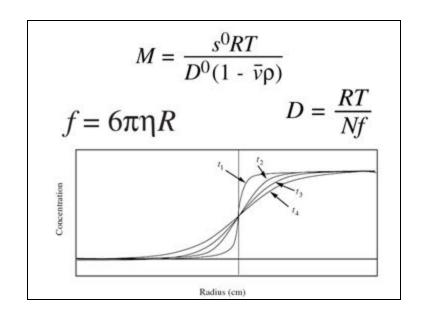
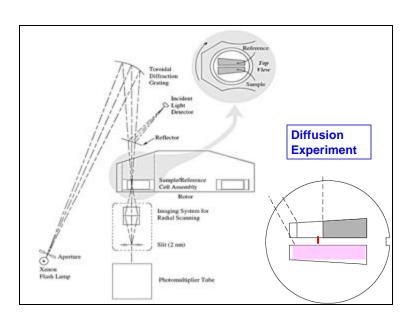
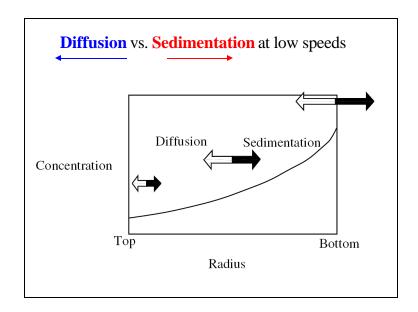
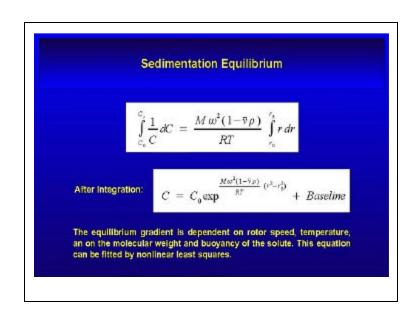


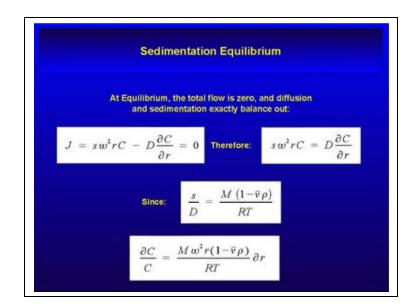
Figure 13. Determination of the diffusion coefficient. The spreading of an initially sharp boundary of human spectrin was followed with time. The slope of the plot of  $[c_p/(dc/dx)]^2$  versus time is  $4\pi$  times the diffusion coefficient.

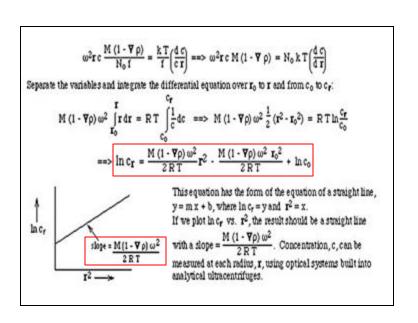


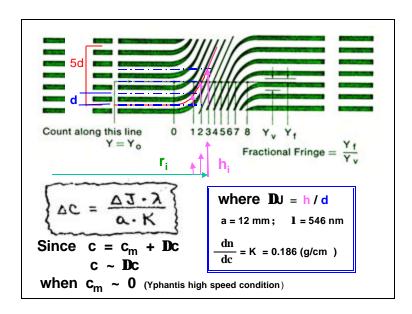












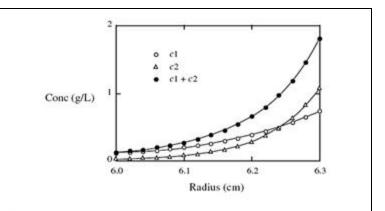


Figure 16. Sedimentation equilibrium distribution of two different solutes. Data were simulated for two species: (a)  $M_r = 40,000$ ; (b)  $M_r = 80,000$ . The angular velocity was 15,000 rpm, and a partial specific volume of 0.73 was assigned to both species. The distribution of total solute concentration in the cell is also shown ( $\bullet$ ).