### **Binding**

### "The secret of life is molecular recognition; the

ability of one molecule to "recognize" another through weak bonding interactions."

Linus Pauling at the 25th anniversary of the Institute of Molecular Biology at the University of Oregon

Binding is the first step necessary for a biological response. Before macromolecules can perform a function, they normally must interact with a specific ligand. In some cases like myoglobin, binding and subsequent release of the ligand might be the sole function of the macromolecule. To understanding binding, we must consider the equilbria involved, how binding is affected by ligand and macromolecule concentration, and how to experimentally analyze and interpret binding data and binding curves.

Hackert – CH370

### **Ligand Binding**

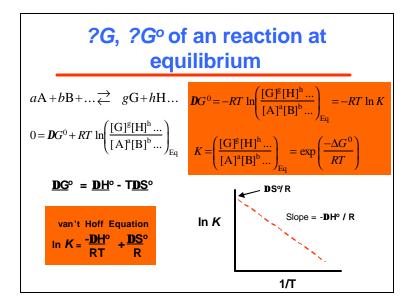
### General description of ligand binding

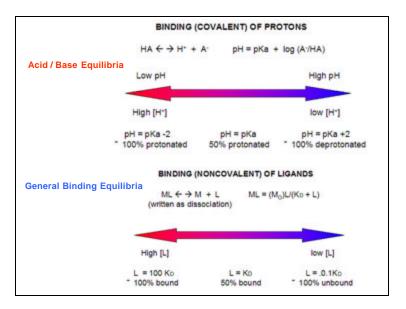
- the essential terms and equations
- equilibrium binding / dissociation constant
- review thermodynamics / van't Hoff plots
- Simple equilibrium binding
  - stoichiometric titration
- · Complex equilibrium binding
  - Multiple sites / cooperativity
  - Microscopic vs. Macroscopic binding constants
  - Scatchard plots and Hill Plots
  - (simple) techniques to determine K

# Summary of Key Equations / Relationships $E + S \hat{U} ES ; \quad for single site$ $K_d = K_{off} / K_{on} = [E][S] / [ES] \text{ and } K_a = 1 / K_d$ $S_o = S + ES; \quad E_o = E + ES$ define Fractional Occupancy of sites $q = [ES] / [E_o] = [ES] / ([E] + [ES]) \times [S] / [S] \times [1 / ES] / [1 / ES]$ then $q = [S] / (K_d + [S])$ thus when [S] = K\_d , then q = 0.50 when [S] = 4K\_d , then q = 0.80 when [S] = 10K\_d , then q = 0.91 Note: [S] = conc. of free ligand!!

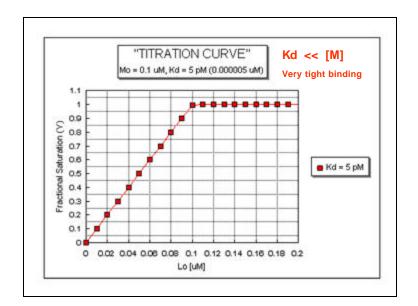
## What is the meaning of the dissociation constant (Kd) for binding of a single ligand to its site?

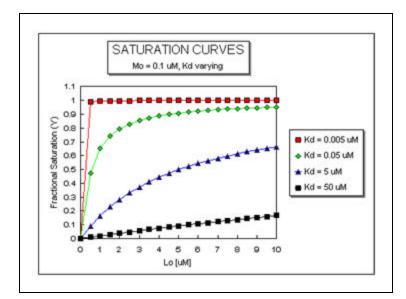
- 1.  $K_d$  has units of concentration, M or mol / liter
- 2.  $K_{d}$  gives the concentration of ligand to saturate 50% of the ligand binding sites (when the total site concentration is much lower than  $K_{d}$ )
- 3. Almost all binding sites are saturated when the free ligand concentration is 10 x  $K_{\rm d}$
- 4. The dissociation constant  $K_{d}$  is related to Gibbs free energy  $?G^{\circ}$  by the relation  $?G^{\circ} = -R T \ln K_{d}$



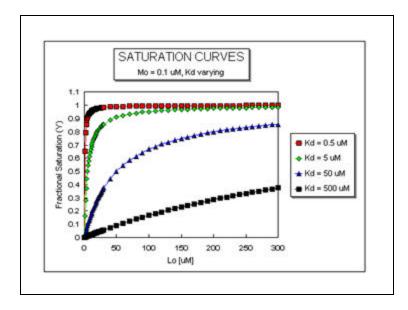


# $K_d$ values in biological systemsMovovalent ions binding to proteins or DNA have $K_d 0.1 \text{ mM}$ to 10 mMAllosteric activators of enzymes e. g. NAD have $K_d 0.1 \mu$ M to 0.1 mMSite specific binding to DNA $K_d 1 \text{ nM}$ to 1 pMTrypsin inhibitor to pancreatic trypsin protease $K_d 0.01 \text{ pM}$ Antibody-antigen interaction have $K_d 0.1 \text{ mM}$ to 0.0001 pM

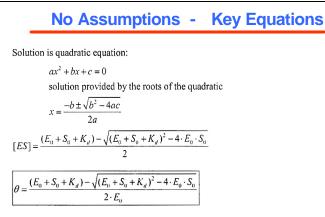




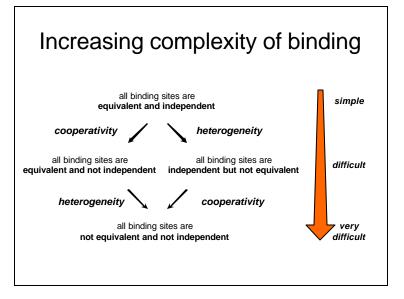
 $\begin{array}{l} \textbf{Simplification of Key Equations} \\ \hline \textbf{E} + \textbf{S} \ \mathbf{\hat{U}} \ \textbf{ES} \ ; \quad \textit{for single site} \\ \textbf{K}_{d} = \textbf{k}_{off} / \textbf{k}_{on} = [\textbf{E}][\textbf{S}] / [\textbf{ES}] \ and \ \textbf{K}_{a} = 1 / \textbf{K}_{d} \\ \hline \textbf{S}_{o} = \textbf{S} + \textbf{ES}; \ \textbf{E}_{o} = \textbf{E} + \textbf{ES} \\ \hline \textbf{If} \ \textbf{S}_{o} >> \textbf{E}_{o} \ , \textbf{then } \textbf{S} \sim \textbf{S}_{o} \\ \textbf{then} \ \textbf{K}_{d} \ [\textbf{ES}] = [\textbf{E}_{o} - \textbf{ES}][\textbf{S}_{o}] \\ [\textbf{ES}] = \textbf{E}_{o} \textbf{S}_{o} / (\textbf{K}_{d} + \textbf{S}_{o}); \\ \textbf{define Fractional Occupancy of sites} \\ \textbf{q} = [\textbf{ES}] / [\textbf{E}_{o}] = [\textbf{ES}] / ([\textbf{E}] + [\textbf{ES}]) = [\textbf{S}_{o}] / (\textbf{K}_{d} + [\textbf{S}_{o}]) \\ \textbf{thus when } [\textbf{S}_{o}] = \textbf{K}_{d} \ , \textbf{then } \textbf{q} = 0.5 \end{array}$ 

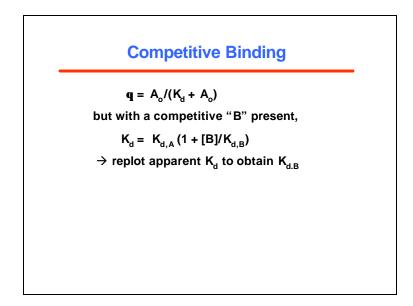


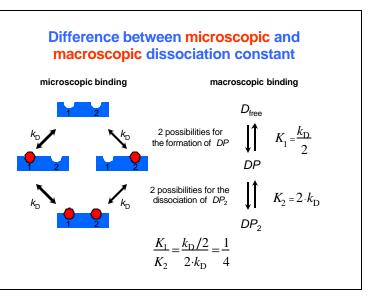
| No Assumptions - Key Equations                                                                          |                                                                                       |
|---------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------|
| Derivation of quadratic equationwith no assumptions concerning substrate concentration.                 |                                                                                       |
| $fraction = \theta = [ES]/[E]_0 = [ES]/([E]+[ES])$                                                      | The derivation starts the same as above                                               |
| $\theta = \frac{K_a[E][S]}{[E] + K_a[E][S]} = \frac{K_a[S]}{1 + K_a[S]} = \frac{[S]}{1 + K_a + [S]}$    | The Fraction of sites bound relative to [S]                                           |
| $\theta = \frac{[S]}{K_d + [S]} = \frac{[S]_0 - [ES]}{K_d + [S]_0 - [ES]} = \frac{[ES]}{[E]_0}$         | ூ Substitution of [S]=[S]₀-[ES]                                                       |
| $[ES](K_d + [S]_0) - [ES]^2 = [E]_0[S]_0 - [ES][E]_0$ $[ES]^2 - [ES](K_d + [S]_0 + [E]_0) + [E]_0[S]_0$ | <sup>∞</sup> Form of equation require solution as the roots of the quadratic equation |
|                                                                                                         |                                                                                       |

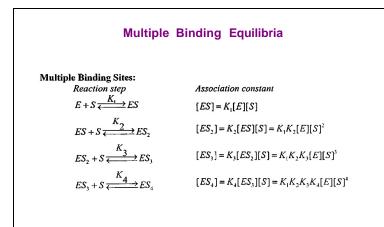


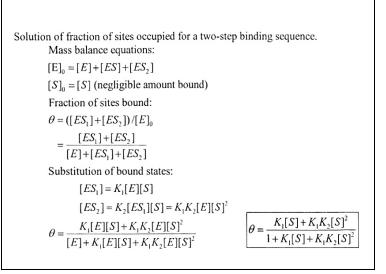
This equation must be used rather than the hyperbola whenever the enzyme concentration is comparable or greater than the dissociation constant. As a general rule, if  $[E]_0$  is less than 5 times the  $K_d$ , the hyperbolic fit is probably adequate.

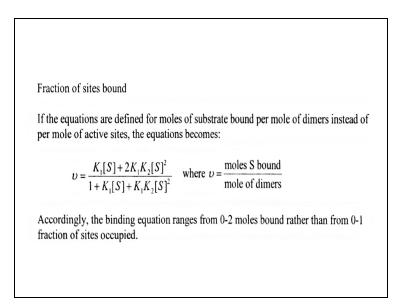




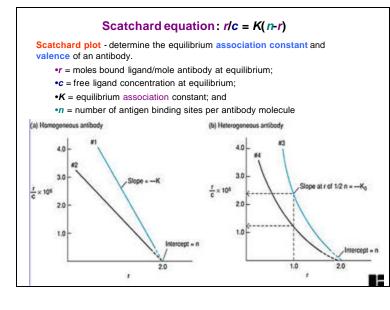








| Manipulations of Equations                                                                                                             |                                                                 |  |
|----------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------|--|
| a) double reciprocal plot                                                                                                              |                                                                 |  |
| $1/q = K_{d}/S_{o} + 1$ ; plot $1/q$ vs. $1/S_{o}$                                                                                     |                                                                 |  |
| b) Scatchard Plot: $\mathbf{q} = \mathbf{S}_{o} / (\mathbf{K}_{d} + \mathbf{S}_{o})$ or                                                |                                                                 |  |
| $\mathbf{q}\mathbf{K}_{d} + \mathbf{q}\mathbf{S}_{o} = \mathbf{S}_{o}$ or $\mathbf{q} = 1 - \mathbf{q}\mathbf{K}_{d} / \mathbf{S}_{o}$ |                                                                 |  |
| plot <b>q</b> vs. <b>q</b> /S <sub>o</sub> slope = - K <sub>d</sub>                                                                    |                                                                 |  |
| Linearized forms of the equation:                                                                                                      |                                                                 |  |
| Double reciprocal plot:                                                                                                                | Skatchard Plot                                                  |  |
| $1/\theta = \frac{[S] + K_d}{[S]} = 1 + \frac{K_d}{[S]}$                                                                               | $\theta = 1 - \frac{\theta K_d}{[S]}$                           |  |
| $\frac{1}{[S]} = \frac{1}{[S]} = 1 + \frac{1}{[S]}$                                                                                    | Or for multiple sites:                                          |  |
| Or for multiple sites:<br>$1/\upsilon = \frac{[S] + K_d}{[S]} = n + \frac{K_d}{[S]}$                                                   | $\theta = n - \frac{\upsilon K_d}{[S]}$                         |  |
|                                                                                                                                        | $\upsilon = \frac{\text{moles bound}}{\text{mole E}} = n\theta$ |  |



### **EXPERIMENTAL DETERMINATION OF Kd**

### **TECHNIQUES THAT REQUIRE SEPARATION OF BOUND FROM FREE**

LIGAND – Care must be given to ensure that the equilibrium of  $M + L \iff ML$  is not shifted during the separation technique.

• gel filration chromatography - Add M to a given concentration of L. Then elute the mixture on a gel filtration column, eluting with the free ligand at the same concentration. The ML complex will elute first and can be quantitated. If you measure the free ligand coming off the column, it will be constant after the ML elutes with the exception of a single dip near where the free L would elute if the column was eluted without free L in the buffer solution. This dip represents the amount of ligand bound by M.

• membrane filtration - Add M to radiolableled L, equilibrate, and then filter through a filter which binds M and ML. For instance, a nitrocellulose membrane binds proteins irreversibly. Determine the amount of radiolabeled L on the membrane which equals [ML].

• precipitation - Add a precipitating agent like ammonium sulfate, which precipitates proteins and hence both M and ML. Determine the amount of ML.

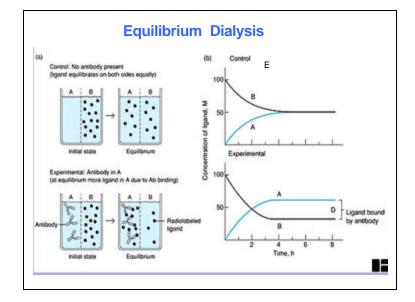
### **EXPERIMENTAL DETERMINATION OF Kd**

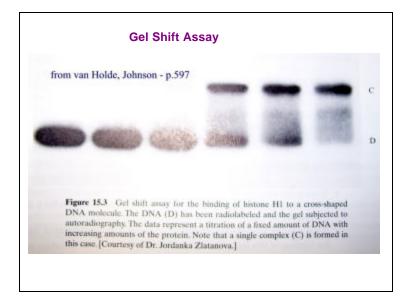
### TECH. THAT DO NOT REQUIRE SEPARATION OF BOUND FROM FREE LIGAND

• equilibrium dialysis - Place M in a dialysis bag and dialyse against a solution containing a ligand whose concentration can be determined using radioisotopic or spectroscopic techniques. At equilibrium, determine free L by sampling the solution surrounding the bag. By mass balance, determine the amount of bound ligand, which for a 1:1 stoichiometry gives ML. Repeat at different ligand concentrations.

• *gel shift assay* – Use autoradiography and gel electrophoresis with radiolabeled macromolecule.

• spectroscopy - Find a ligand whose absorbance or fluorescence spectra changes when bound to M. Alternatively, monitor a group on M whose absorbance or fluorescence spectra changes when bound to L.





### Spectroscopy

### Fluorescence data

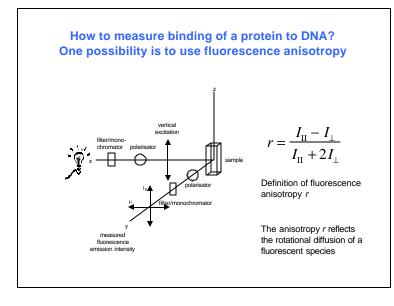
$$F = F_0 + \Delta F \cdot \theta$$

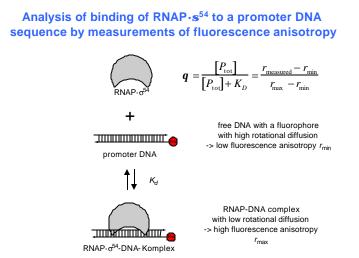
where  $\Delta F = F_{\infty} - F_0$ and  $\theta$  is defined by either:

$$\theta = \frac{[S]_0}{K_d + [S]_0} \qquad \text{OR...}$$

 $^{\infty}$  This equation normalizes the observable signal to a scale that can be related to fractional occupancy,  $\theta$ .

$$\theta = \frac{(E_0 + S_0 + K_d) - \sqrt{(E_0 + S_0 + K_d)^2 - 4 \cdot E_0 \cdot S_0}}{2 \cdot E_0}$$





Note: DNA binding examples from Karsten Rippe - Heidelberg

