

# X-Ray Crystallography

*“If a picture is worth a thousand words, then a macromolecular structure is priceless to a physical biochemist.” – van Holde*

Topics:

## 1. Protein Data Bank (PDB)

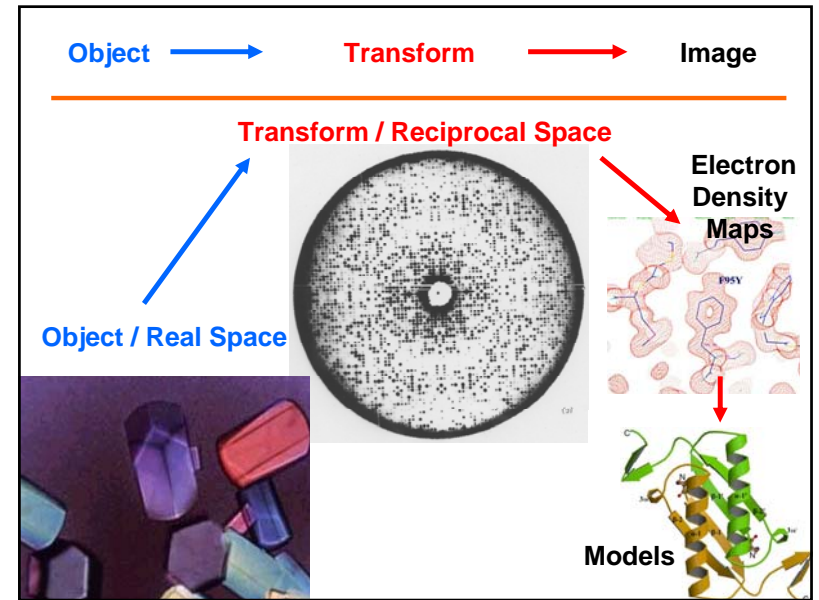
Data mining and Protein Structure Analysis Tools

## 2. Image Formation

Resolution / Wavelength (Amplitude, Phase) / Light Microscopy / EM / X-ray / (NMR)

## 3. X-Ray Crystallography (after NMR)

- Crystal Growth – Materials / Methods
- Crystal Lattices - Lattice Constants / Space Groups / Asymmetric Unit
- X-ray Sources – Sealed Tube / Rotation Anode / Synchrotron
- Theory of Diffraction – Bragg's Law / Reciprocal Space
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- Structure Solution – Phase Problem: MIR / MR / MAD
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- Analysis and presentation of results



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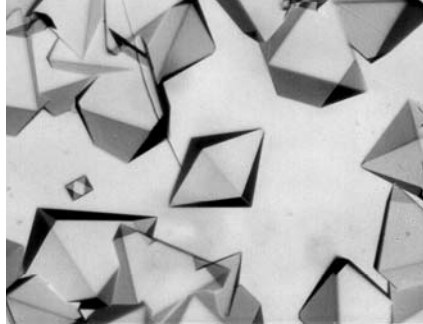
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**Glucose Isomerase Crystals**

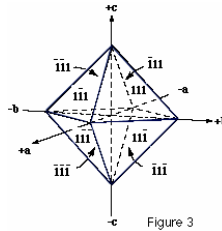
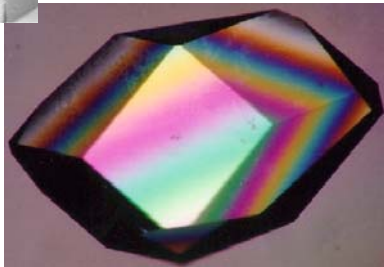
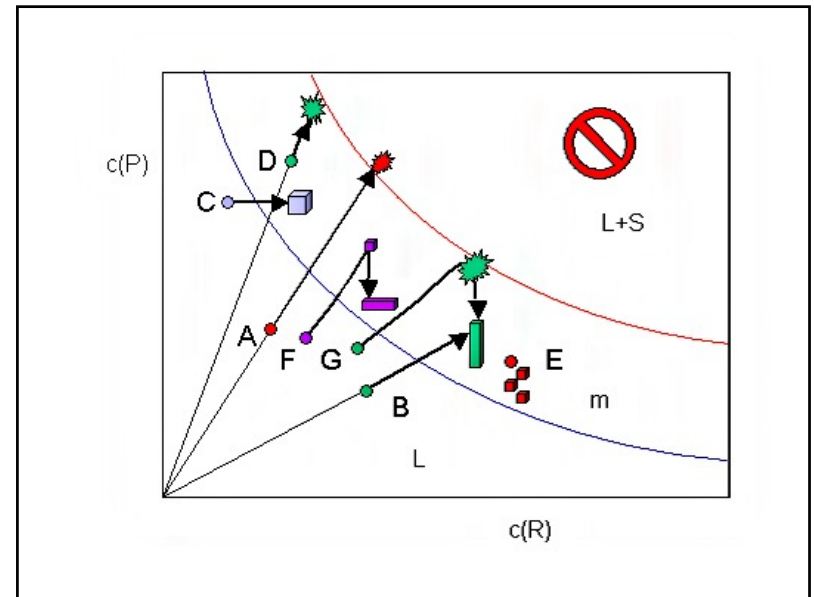








Figure 3



**Lysozyme Crystals**





**Types of Crystals**  
 Welcome to the Home Page of Terese Bergfors  
 "The Protein Crystallization Page" <http://xray.bmc.uu.se/~terese/>

	<b>Sea urchins.</b> These often begin as spherulites (see <a href="#">joining tubules</a> ) or grow from a spherulite. They are extremely thin needles clustered around a single nucleation site. Often they appear "fuzzy". The white arrows in this picture show three-dimensional crystals growing from independent nucleation sites in the same drop.
	<b>Needles.</b>
	Extremely thin needles growing from a single nucleation center. Since these needles are much longer, I would not call this a "sea urchin" any longer. Notice the large 3-D crystal growing in the same drop.
	<b>Needles.</b> Still too many but at least they are single needles. The nucleation rate is too high which is why you have too many, and too thin. Try reducing the protein or precipitant concentration or both. Another method is to put a layer of oil over the reservoir in the vapor drop set-up. (see Chayen, put reference here). See also the Tutorial 4 on seeding.
	<b>Plates.</b> Two-dimensional. Plates are usually considered an improvement over needles. These are growing from a single nucleation site and overlapping each other, which is far from optimal. Optimize to grow them as separately and thicker.
	<b>A three dimensional crystal.</b> But check the diffraction before you get out the champagne.

**Welcome to the Home Page of Terese Bergfors**  
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<http://xray.bmc.uu.se/~terese/>

**Tutorial 1. Appearances can be deceiving!**

The first thing you should learn is that the appearance (habit, morphology, etc.) of your crystal is NOT what is important. Beautiful-looking crystals may not diffract and ugly ugly crystals might diffract excellently. The only definitive proof of a "GOOD" crystal is its diffraction pattern in the X-ray beam. Therefore, do not be misled by the appearance of your crystal-mount it and check it in the beam.

	<b>Beauty is only skin deep.</b> Don't be fooled by appearances. These crystals may look nice, but they don't diffract.
	These are ugly. In fact they are so ugly you probably wouldn't even bother to mount them but they diffract to LGA. Most of the story don't always go by the appearance of your crystals. It is the X-ray diffraction pattern that counts. With that said, you can now continue the tutorial on interpreting your crystallization drop.

- Variables that influence crystal growth**
1. Nature of macromolecule – Purity and concentration of macromolecule
  2. Nature and concentration of precipitant
  3. pH / Temperature / Pressure
  4. Level of reducing agent or oxidant
  5. Substrates, coenzymes, and ligands / Metal ions
  6. Preparation and storage of macromolecule / Proteolysis and fragmentation
  7. Age of macromolecule / Degree of denaturation
  8. Vibration and sound
  9. Volume of crystallization sample
  10. Seeding
  11. Amorphous precipitate
  12. Buffers
  13. Cleanliness
  14. Organism or species from which the macromolecule was isolated
  15. Gravity, gradients and convection

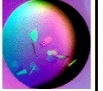
## Common Compounds used in Crystallization

Ammonium or sodium sulfate  
 Sodium or ammonium citrate  
 Sodium or ammonium acetate  
 Magnesium sulfate  
 Cetyltrimethyl ammonium salts  
 Polyethylene glycol 400, 1000, 4000, 6000, 15,000 (now also 2,000, 8,000, etc.)

## Methods for protein crystallization

Batch crystallization (simply dump reagents together)  
 Liquid-liquid diffusion in a capillary tube  
 Vapor diffusion-the most successful method (hanging drop, sitting drop), typically using a Limbro plate. Equilibration occurs between the liquid and vapor phase.  
 Dialysis

## Hampton Crystal Screen Solutions



### Note :

A mini-screen can be set up from the most successful conditions. Those are indicated in the column labeled Miniscreen.

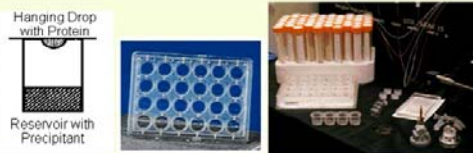
- [a nice list of detergents](#) commonly used in crystallization experiments.
- [matrix encodes](#)
- [CRYSTOOL](#) efficient random screen made for you here on the WEB.

Tube #	SALT	BUFFER	Precipitant	Miniscreen	Tube #
1	0.02M Calcium Chloride	0.1M Na Acetate pH 4.6	30% w/v 2-methyl-2,4-pentanediol	Y	1
2	None	None	0.4M K <sub>2</sub> Na Tartrate tetrahydrate		2
3	None	None	0.4M Ammonium dihydrogen phosphate		3
4	None	0.1M Tris-HCl pH 8.5	2.0M Ammonium Sulfate	Y	4
5	0.2M tri-sodium citrate	0.1M Na HEPES pH 7.5	30% w/v 2-methyl-2,4-pentanediol		5
6	0.2M Magnesium chloride	0.1M Tris-HCl pH 8.5	30% w/v PEG 4000		6
7	None	0.1M Na Cacodylate pH 6.5	1.4M Sodium acetate trihydrate		7
8	0.2M tri-sodium citrate	0.1M Na Cacodylate pH 6.5	30% w/v 2-propanol		8
9	0.2M Ammonium acetate	0.1M Na Citrate pH 5.6	30% w/v PEG 4000	Y	9
10	0.2M Ammonium acetate	0.1M Na Acetate pH 4.6	30% w/v PEG 4000	Y	10
11	None	0.1M Na Citrate pH 5.6	1.0M Ammonium dihydrogen phosphate		11
12	0.2M Magnesium chloride	0.1M Na HEPES pH 7.5	30% w/v 2-propanol		12
13	0.2M tri-sodium citrate	0.1M Tris-HCl pH 8.5	30% w/v PEG 400		13
14	0.2M Calcium Chloride	0.1M Na HEPES pH 7.5	28% w/v PEG 400	Y (best)	14
15	0.2M Ammonium acetate	0.1M Na Cacodylate pH 6.5	30% w/v PEG 8000		15
16	None	0.1M Na HEPES pH 7.5	1.5M Lithium sulfate monohydrate	Y	16
17	0.2M Lithium sulfate	0.1M Tris-HCl pH 8.5	30% w/v PEG 4000	Y (2nd best)	17

## Hanging Drop Method - Crystal Screening

### The Experimental Setup

In order to obtain a crystal, the protein molecules must assemble into a periodic lattice. One starts with a solution of the protein with a fairly high concentration (2-50 mg/ml) and adds reagents that reduce the solubility close to spontaneous precipitation. By slow further concentration, and under conditions suitable for the formation of a few nucleation sites, small crystals may start to grow. Often very many conditions have to be tried to succeed. This is usually done by **initial screening**, followed by a systematic optimization of conditions. Crystals should be a few tenths of a mm in each direction to be useful for diffraction experiments.



Right: The hanging drop technique. Center: 24 such hanging drop experiments are set up in a Limbro plate. Right: A kit of different screening solutions, a set-up Limbro plate, dialysis buttons and a micro batch plate behind a goniometer head.

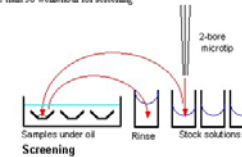
The most common setup to grow protein crystals is by the **hanging drop** technique: A few microliters of protein solution are mixed with an about equal amount of reservoir solution containing the precipitants. A drop of this mixture is put on a glass slide which covers the reservoir. As the protein/precipitant mixture in the drop is less concentrated than the reservoir solution (remember we mixed the protein solution with the reservoir solution about 1:1), water evaporates from the drop into the reservoir. As a result the concentration of both protein and precipitant in the drop slowly increases, and crystals may form. There is a variety of other techniques available such as sitting drops, dialysis buttons, and gel and microbatch techniques. Robots are useful for automatic **screening** and optimization of crystallization conditions. We have implemented a web computing service of **Bruno Szabolcs's CRYSTOOL**, an inherently efficient random screen for crystallization conditions that you can customize. The main advantage is the small sample size a **crystallization robot** can handle reproducibly, but it needs some effort to set it up. Click here to learn more about the **IMPACT** robot.

## Using Oryx 6 for Crystallization with Microbatch

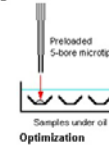
Microbatch operation is identical to **IMPAX 1-5**

<http://www.douglas.co.uk/oryx.htm>

**Very Fast: 240 wells/hour**  
 more than 50 wells/hour for screening



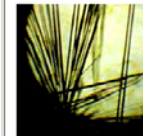
**Uses little protein**  
 0.1 - 1 µl per well



**Microbatch screening finds more leads**  
 than VD in a given time

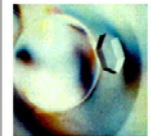
	Automated MB	Manual VD
Proteins screened	6	6
Screening solutions	48	48
Runs	3	1
Volume per well	1 + 1 µl	4 + 4 µl
Total protein used	864 µl	1152 µl
Operator time	3 hr	24 hr
Crystallization conditions found	43	41
Unique conditions	17	15

**Large diffracting**

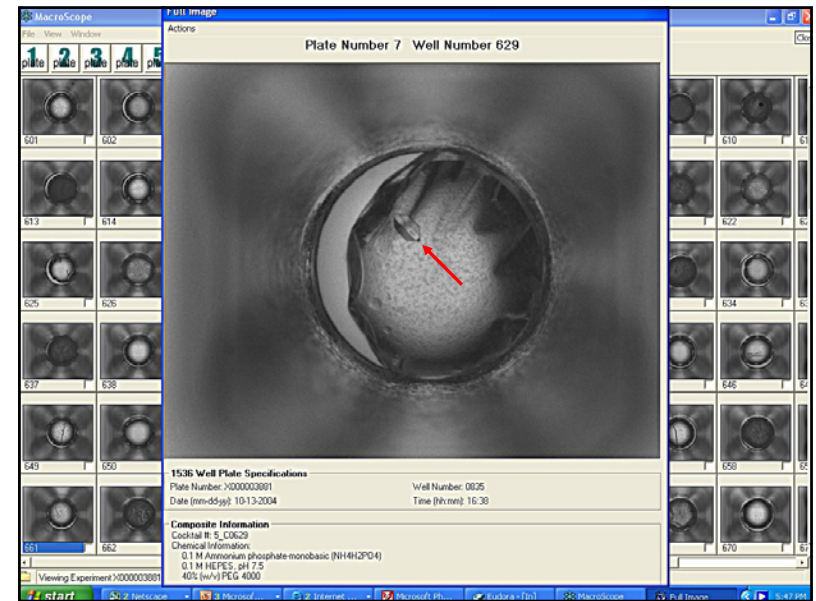
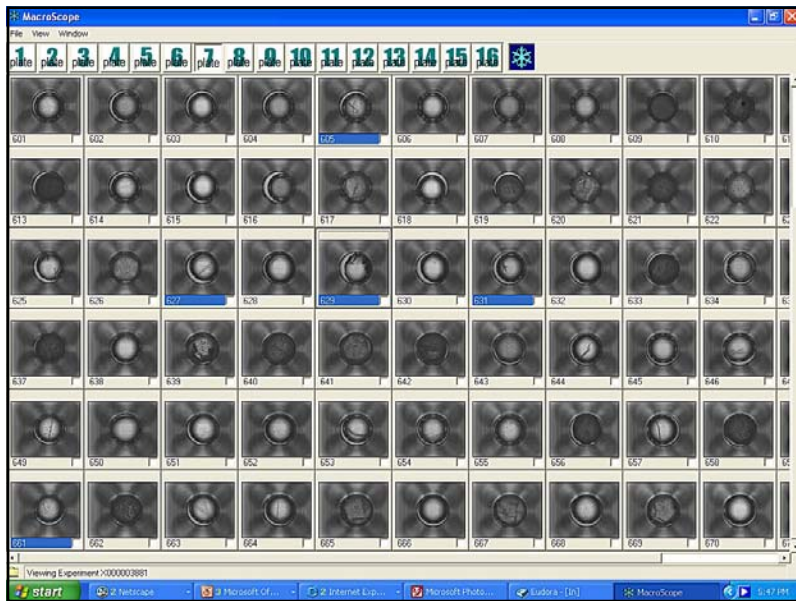


MB crystals of antibody hA20.1. Data could not be collected from 10 crystals which were available. Courtesy of E. Conti. Acta Crystallographica, D 52 (1996), 4, pp 616-619. <http://www.douglas.co.uk/oryx2.htm>

**crystals**



MB crystals of ribbed polydipropylene from a thermophilic bacterium. Courtesy of Y. Zaslavsk. Acta Crystallographica, D 52 (1996), pp 882-886. <http://www.douglas.co.uk/oryx2.htm>



HisJ - His complex:

Tetanus Toxin C Fragment:

[http://www.ccp14.ac.uk/ccp/web-mirrors/lnlrupp/crystal\\_lab/Cryst\\_lab.html](http://www.ccp14.ac.uk/ccp/web-mirrors/lnlrupp/crystal_lab/Cryst_lab.html)

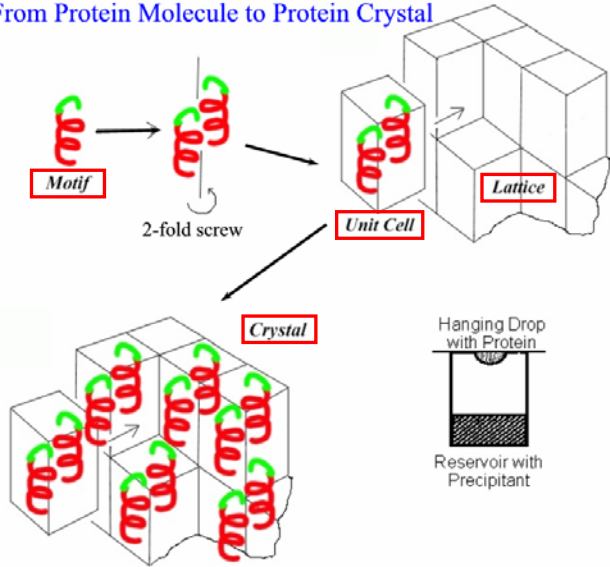
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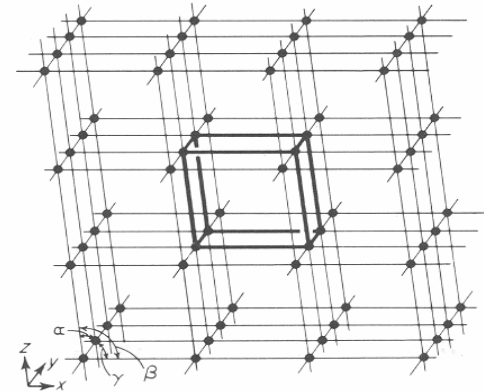
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### From Protein Molecule to Protein Crystal



A **unit cell** is defined by its lattice constants:

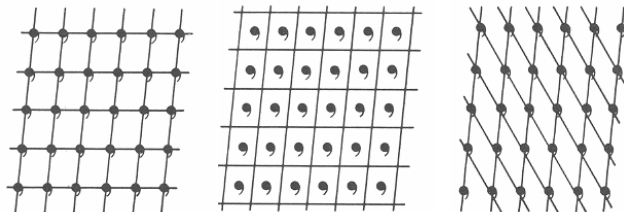
**a, b, c** and  **$\alpha, \beta, \gamma$**



### How to identify “the” **unit cell** ?



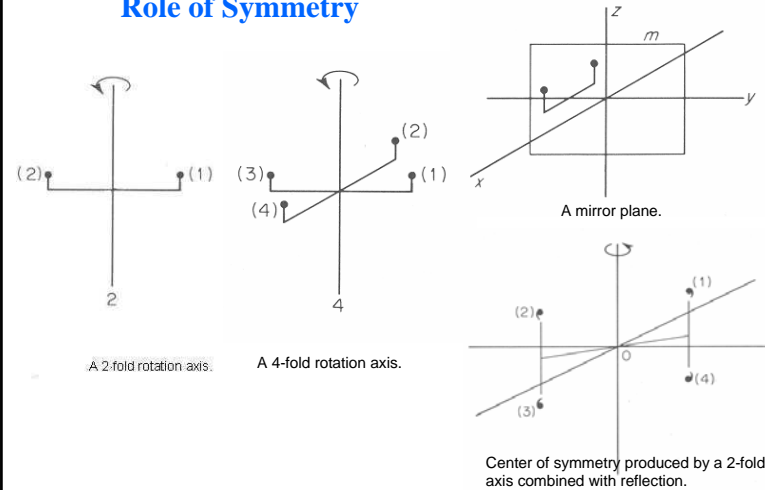
Regular two-dimensional array.



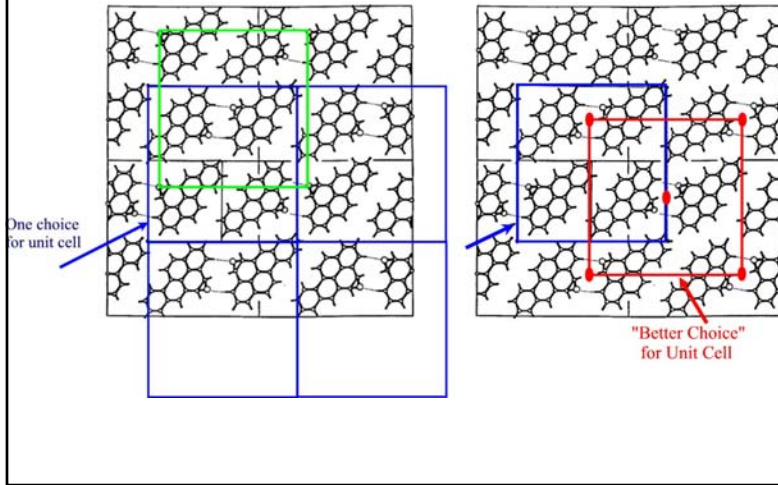
Three different grid systems referred to the array same array.

### How to identify “the” **unit cell** ?

#### Role of Symmetry



### Unit Cell Selection is Based on Symmetry



## The Fourteen Bravais Lattices

There are fourteen distinct space groups that a Bravais lattice can have. Thus, from the point of view of symmetry, there are fourteen different kinds of Bravais lattices. **Auguste Bravais (1811-1863)** was the first to count the categories correctly.



### Crystal Systems

Crystal System	Bravais Type(s)	External Minimum Symmetry	Unit Cell Properties
Tetragonal	P	None	a, b, c, a, b, c, ga
Monoclinic	P, C	One 2-fold axis, parallel b (b unique)	a, b, c, 90, b, 90
Orthorhombic	P, I, F	Three perpendicular 2-folds	a, b, c, 90, 90, 90
Tetragonal	P, I	One 4-fold axis, parallel c	a, a, c, 90, 90, 90
Trigonal	P, R	One 3-fold axis	a, a, c, 90, 90, 120
Hexagonal	P	One 6-fold axis	a, a, c, 90, 90, 120
Cubic	P, F, I	Four 3-folds along space diagonal	a, a, a, 90, 90, 90

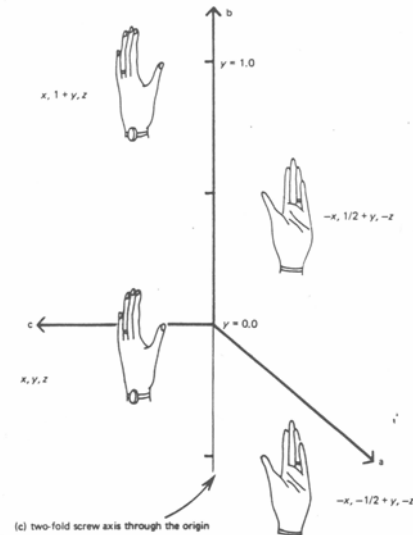
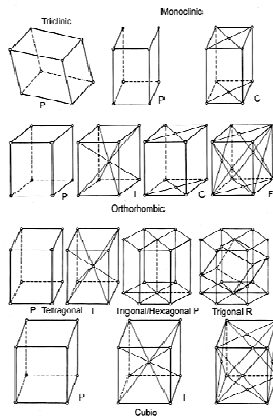
Symmetry operations: 1, 2, 3, 4, 6, -1, -2, -3, -4, -6, m


Crystal System	Point groups	Lattice Class	Patterson Symmetry
Tetragonal	1, -1	-1	P-1
Monoclinic	2, m, 2/m	2/m	P2/m, C2/m
Orthorhombic	222, mm2, mmm	mmm	Pmm, Cmm, Fmm, Immm
Tetragonal	4, -4, 4/m, -42, 4mm, -42m, 4/mmm	4/m, 4/mmm	P4/m, I4/m, P4/mmm, I4/mmm
Trigonal	3, -3, 32, 3m, -3m	-3, 3m	P-3, R-3, P-3m1, P-31m, R-3m
Hexagonal	6, -6, 6/m, -62, 6mm, -62m, 6/mmm	6/m, 6/mmm	P6/m, P6/mmm
Cubic	23, m-3, 432, -43m, m3m	m-3, m-3m	Pm-3, Im-3, F-3m, Pm-3m, Fm-3m, Im-3m

#### Notes

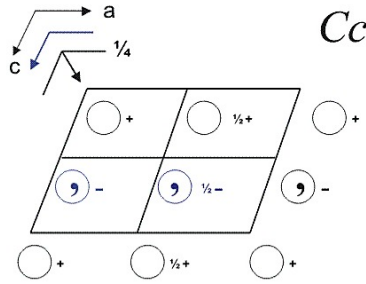
- Lattice class corresponds to symmetry of reciprocal space (diffraction pattern)
- Patterson symmetry is Lattice class plus allowed Bravais centering, i.e. centrosymmetric and symorphic

### The 14 Bravais Lattices






Carl Hermann

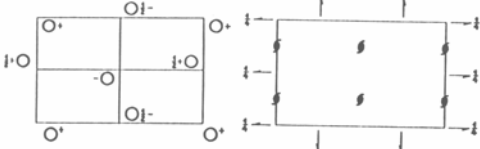


**Cc No.9**



Charles-Victor Mauguin

Orthorhombic 222



Origin halfway between three pairs of non-intersecting screw axes

$P2_1 2_1 2_1$

No. 19

$P2_1 2_1 2_1$   
 $D_2^4$

Number of positions, Wyckoff notation, and point symmetry

4 *a* | *x, y, z*;  $\bar{1}-x, \bar{y}, \bar{z}$ ;  $\bar{1}+x, \bar{1}-y, \bar{z}$ ;  $\bar{1}, \bar{1}+y, \bar{1}-z$ .

Co-ordinates of equivalent positions

Conditions limiting possible reflections


$hkl$ : No conditions  
 $0kl$ :  
 $h0l$ :  
 $h\bar{h}0$ :  
 $h00$ :  $h=2n$   
 $0k0$ :  $k=2n$   
 $00l$ :  $l=2n$

Symmetry of special projections

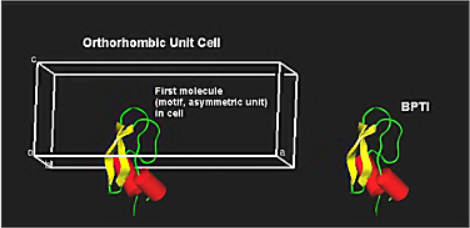
(001) *pgg*;  $a'-a, b'-b$       (100) *pgg*;  $b'-b, c'-c$       (010) *pgg*;  $c'-c, a'-a$

**FIGURE 7.2** Part of a Page from "International Tables for X-Ray Crystallography," Volume I.

### BPTI Space Group P212121



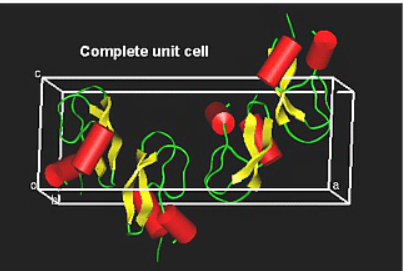
Asymmetric Unit



Orthorhombic Unit Cell

First molecule (motif, asymmetric unit) in cell

BPTI



Complete unit cell

**TABLE 3.4 Space Groups in Standard Orientations\***

System	Point Group	Space Group				Fraction		
Triclinic	$\bar{1}$	P1				$\frac{1}{2}$		
	$\bar{1}$	P1						
Monoclinic	2	P2	C2			$\frac{1}{4}$		
	m	Pm	Cm					
	2/m	P2/m	C2/m	Cc	P2/c	C2/c		
Orthorhombic	222	P222	P2,2,2	P2,2,2	C222	C222	$\frac{1}{8}$	
	mm2	Pmm2	Pmm2	Pmm2	Pma2	Pma2		
	mmm	Pmm	Pmm	Pmm	Pmm	Pmm	Pmm	
		Pmm	Pmm	Pmm	Pmm	Pmm	Pmm	
	Tetragonal	4	P4	P4		I4	I4	$\frac{1}{8}$
		4/m	P4/m	P4/m	P4/m	P4/m	I4/m	$\frac{1}{16}$
		422	P422	P4,2,2	P4,2,2	P4,2,2	P4,2,2	
		4mm	P4mm	P4mm	P4mm	P4mm	P4mm	
	Trigonal/rhombohedral	3	P3	P3		R3		$\frac{1}{6}$
		32	P312	P312	P3,12	P3,12	P3,12	$\frac{1}{12}$
Hexagonal	6	P6	P6		P6	P6	$\frac{1}{12}$	
	6/m	P6/m	P6/m		P6/m	P6/m		
	622	P622	P6,2,2	P6,2,2	P6,2,2	P6,2,2	$\frac{1}{24}$	
Cubic	23	P23	P23		I23	I23	$\frac{1}{24}$	
	m3	Pm3	Pm3		Fm3	Fm3	$\frac{1}{48}$	
	432	P432	P4,3,2	P4,3,2	F4,3,2	F4,3,2	$\frac{1}{48}$	

\*The 11 Laue symmetries are separated by horizontal lines.

TABLE 16-5 The 65 "Biological" Space Groups

CRYSTAL SYSTEM	LAT-TICE	MINIMUM SYMMETRY OF UNIT CELL	UNIT CELL EDGES AND ANGLES*	DIFFRACTION PAT-TERN SYM-METRY*	SPACE GROUPS*
Triclinic	<i>P</i>	None	$a \neq b \neq c$ $\alpha \neq \beta \neq \gamma$	$\bar{1}$	<i>P1</i>
Monoclinic	<i>P</i>	2-fold axis parallel to <i>b</i>	$a \neq b \neq c$ $\alpha = \gamma = 90^\circ$ $\beta \neq 90^\circ$	<i>2m</i>	<i>P2, P2<sub>1</sub></i>
	<i>C</i>				<i>C2</i>
Orthorhombic	<i>P</i>	3 mutually perpendicular 2-fold axes	$a \neq b \neq c$ $\alpha = \beta = \gamma = 90^\circ$	<i>mmm</i>	<i>P222, P2<sub>2</sub>2<sub>2</sub>, P222<sub>1</sub>, P2<sub>1</sub>2<sub>1</sub>2</i>
	<i>C</i>				<i>C222, C222<sub>1</sub></i>
	<i>I</i>				<i>[I222, I2<sub>1</sub>2<sub>1</sub>2<sub>1</sub>]</i>
Tetragonal	<i>P</i>	4-fold axis parallel to <i>c</i>	$a = b \neq c$ $\alpha = \beta = \gamma = 90^\circ$	<i>4m</i>	<i>P4, (P4<sub>1</sub>, P4<sub>2</sub>), P4<sub>3</sub></i>
	<i>I</i>				<i>I4, I4<sub>1</sub></i>
	<i>F</i>				<i>P422, (P4<sub>2</sub>22, P4<sub>2</sub>2<sub>1</sub>), P4<sub>2</sub>2<sub>2</sub></i>
Trigonal/rhombohedral	<i>R<sup>h</sup></i>	3-fold axis parallel to <i>c</i>	$a = b = c$ $\alpha = \beta = \gamma \neq 90^\circ$	$\bar{3}$	<i>P422, (P4<sub>2</sub>22, P4<sub>2</sub>2<sub>1</sub>), P4<sub>2</sub>2<sub>2</sub></i>
	<i>P<sup>h</sup></i>				<i>R3</i>
	<i>F<sup>h</sup></i>				<i>P3, (P3<sub>1</sub>, P3<sub>2</sub>)</i>
Hexagonal	<i>P</i>	6-fold axis parallel to <i>c</i>	$a = b \neq c$ $\alpha = \beta = 90^\circ$ $\gamma = 120^\circ$	<i>6m</i>	<i>R32</i>
					<i>[P321, P312]</i>
					<i>[(P3<sub>1</sub>21, P3<sub>2</sub>21), (P3<sub>1</sub>12, P3<sub>2</sub>12)]</i>
Cubic	<i>P</i>	3-fold axes along cube diagonals	$a = b = c$ $\alpha = \beta = \gamma = 90^\circ$	<i>m3</i>	<i>P6<sub>3</sub>, (P6<sub>3</sub>, P6<sub>6</sub>)</i>
					<i>P622, (P6<sub>2</sub>22, P6<sub>2</sub>2<sub>1</sub>)</i>
					<i>P622, (P6<sub>2</sub>22, P6<sub>2</sub>2<sub>1</sub>)</i>
	<i>I</i>			<i>m3m</i>	<i>P23</i>
					<i>P2<sub>1</sub>3</i>
					<i>[I23, I2<sub>1</sub>3]</i>
	<i>F</i>				<i>I23</i>
					<i>P432, (P4<sub>3</sub>32, P4<sub>3</sub>3<sub>2</sub>)</i>
					<i>P4<sub>3</sub>22</i>

# X-Ray Crystallography

*"If a picture is worth a thousand words, then a macromolecular structure is priceless to a physical biochemist."* – van Holde

Topics:

## 1. Protein Data Bank (PDB)

Data mining and Protein Structure Analysis Tools

## 2. Image Formation

Resolution / Wavelength (Amplitude, Phase) / Light Microscopy / EM / X-ray / (NMR)

## 3. X-Ray Crystallography (after NMR)

a) Crystal Growth – Materials / Methods

b) Crystal Lattices - Lattice Constants / Space Groups / Asymmetric Unit

c) X-ray Sources – Sealed Tube / Rotation Anode / Synchrotron

d) Theory of Diffraction – Bragg's Law / Reciprocal Space

e) Data Collection – Methods / Detectors / Structure Factors

f) Structure Solution – Phase Problem: MIR / MR / MAD

h) Refinements and Models

i) Analysis and presentation of results

## X-ray tubes: the "sealed" tube

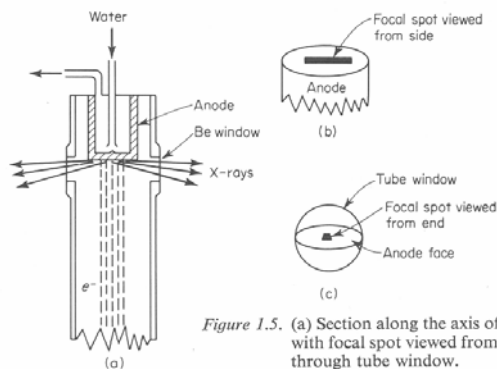
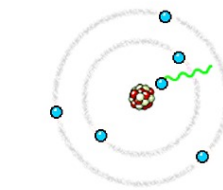


Figure 1.5. (a) Section along the axis of an X-ray tube. (b) Anode with focal spot viewed from side. (c) Focal spot viewed through tube window.

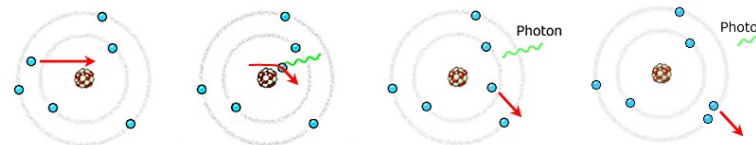
## Origin of Non-characteristic X-rays

### Bremsstrahlung X-rays

In an X-ray tube the electrons emitted from the anode are accelerated towards the metal target cathode by an accelerating voltage of typically 50 kV. The high energy electrons interact with the atoms in the metal target. Sometimes the electron comes very close to a nucleus in the target and is deviated by the electromagnetic interaction. In this process, which is called bremsstrahlung (braking radiation), the electron loses much energy and a photon (X-ray) is emitted. The energy of the emitted photon can take any value up to a maximum corresponding to the energy of the incident electron.



The electron (much lighter than the nucleus) comes very close to the nucleus and the electromagnetic interaction causes a deviation of the trajectory where the electron loses energy and an X-ray photon is emitted.





## Origin of characteristic X-rays

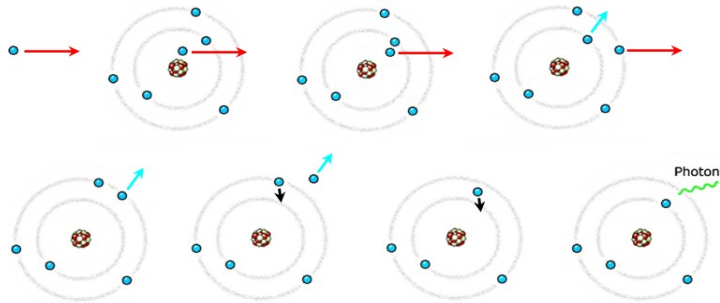
### Characteristic X-ray Lines

The high energy electron can also cause an electron close to the nucleus in a metal atom to be knocked out from its place. This vacancy is filled by an electron further out from the nucleus. The well defined difference in binding energy, characteristic of the material, is emitted as a monoenergetic photon. When detected this X-ray photon gives rise to a characteristic X-ray line in the energy spectrum. C. Barkla observed these lines in 1908-09 and was given the 1917 Nobel Prize for this discovery. He also made the first experiments suggesting that the X-rays are electromagnetic waves.

### Related Laureate



The Nobel Prize in Physics 1917 - Charles Glover Barkla »



## Characteristic X-rays arise from electronic transitions

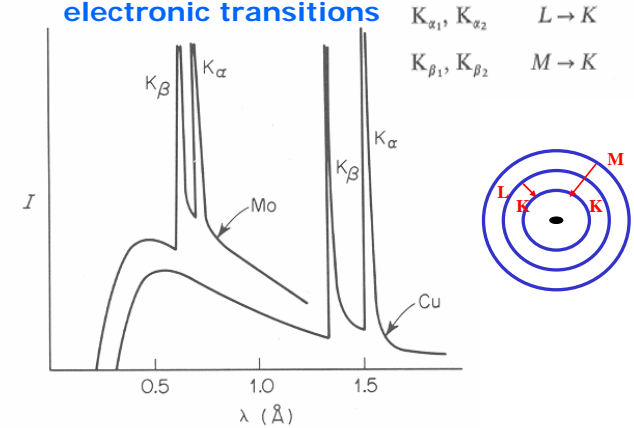


Figure 1.2. X-ray spectra with characteristic peaks: MoK $\alpha$ , 50 Kv; CuK $\alpha$ , 35 Kv.

## Characteristic X-rays have defined $\lambda$

Table 1.1. Target Materials and Associated Constants

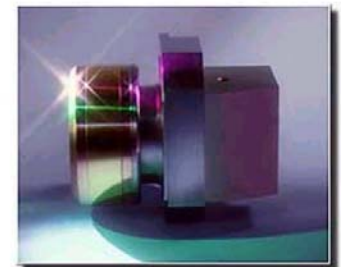
	Cr	Fe	Cu	Mo
Z	24	26	29	42
$\alpha_1, \text{Å}$	2.2896	1.9360	1.5405	0.70926
$\alpha_2, \text{Å}$	2.2935	1.9399	1.5443	0.71354
$\bar{\alpha}, \text{Å}$	2.2909	1.9373	1.5418	0.71069
$\beta_1, \text{Å}$	2.0848	1.7565	1.3922	0.63225
$\beta$ , filt.	V, 0.4 mil†	Mn, 0.4 mil	Ni, 0.6 mil	Nb, 3 mils
$\alpha$ , filt.	Ti	Cr	Co	Y
Resolution, Å	1.15	0.95	0.75	0.35
Critical potential, kV	5.99	7.11	8.98	20.0
Operating conditions, kV:	30–40	35–45	35–45	50–55
half- or full-wave-	10	10	20	20
rectified, mA				
constant potential, mA	7	7	14	14

\*  $\bar{\alpha}$  is the intensity-weighted average of  $\alpha_1$  and  $\alpha_2$  and is the figure usually used for the wavelength when the two lines are not resolved.

† 1 mil = 0.001 inch = 0.025 mm.

## X-ray Generators

FR591



### FR591 Rotating Anode X-ray Generator

The Nomax FR591 rotating anode X-ray generator now has dramatically improved the performance of the anode, by a complete redesign. We now have a static shaft and a rotating anode, instead of rotating both. The cooling water flow has also been redesigned to give much higher throughput, higher flow and higher turbulence, which results in better heat transfer and hence better cooling capacity.

Now with the new ULTRA anode you can get 6 kW on a 0.3mm focus!

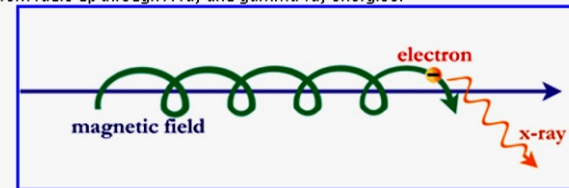


## Another Source of "X-rays"

### Synchrotron Radiation

X-ray photons can also be created under different conditions. When physicists were operating the first particle accelerators, they discovered that electrons can produce photons without colliding at all. This was possible because the magnetic field in the accelerators was causing the electrons to move in large spirals around magnetic field lines of force. This process is called synchrotron radiation.

In the cosmos particles such as electrons can be accelerated to high energies— near the speed of light— by electric and magnetic fields. These high-energy particles can produce synchrotron photons with wavelengths ranging from radio up through X-ray and gamma-ray energies.



Synchrotron Radiation: Electrons moving in magnetic field radiate photons.

## "X-ray" Sources: Beyond X-ray tubes

The **brilliance** of a light source is defined as the number of photons emitted per second, per unit source size, per unit space angle and for a bandwidth of 1/1000 of the photon energy

The comparison between various sources of X-rays shows large differences in their brilliance.

#### X-ray tubes:

Wilhelm Conrad Röntgen discovered X-rays in 1895 whilst working with cathode-ray tubes. Using the principle of fast electrons hitting a metallic target, a first substantial gain in brilliance was not obtained until the introduction of rotating anode sources (~1960).

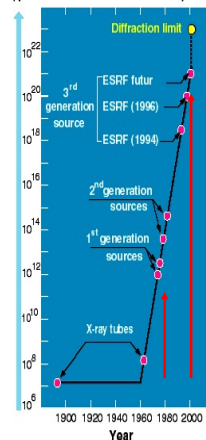
#### Synchrotron Radiation Facilities:

The progress of high energy physics, with the construction of powerful particle accelerators gave birth to what we now call *first generation synchrotron sources* (~1970). Using the deflection of high energy electrons by a magnetic field for the production of X-rays proved so promising that a number of dedicated *second generation sources* were built (~1980). Relying on the combination of *needle* than electron beams and *insertion devices*, *third generation synchrotron sources* (~1995) are now emitting synchrotron X-ray beams that are a trillion ( $10^{12}$ ) times more brilliant than those produced by X-ray tubes.

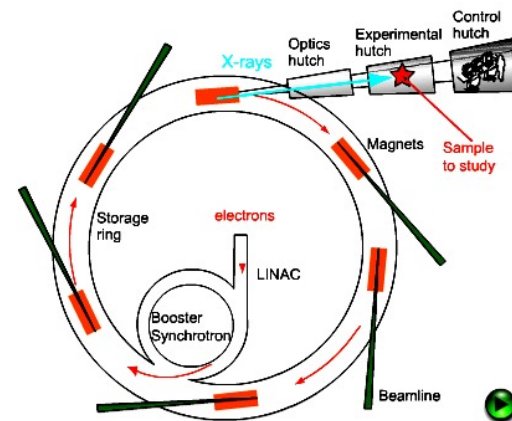
#### Free Electron X-ray Lasers:

Coupling electron and X-ray beams together, the Free Electron X-ray Lasers currently on the drawing boards could be the next generation of X-ray sources. While they promise to achieve an increase in peak brilliance by another factor of a trillion, the first prototypes may be operational around the year 2010.

Brilliance of the X-ray beams  
(photons / s / mm<sup>2</sup> / mrad<sup>2</sup> / 0.1% BW)

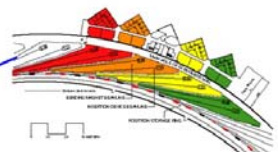
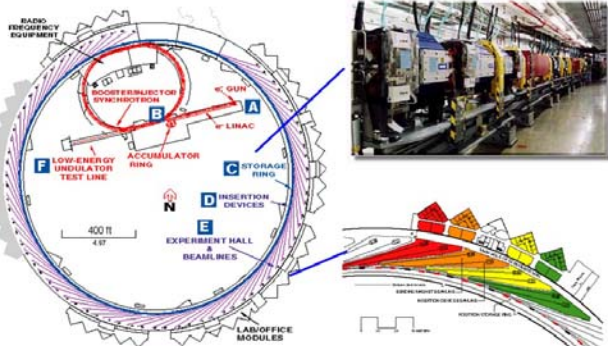


## How synchrotron light is produced?





APS - Advanced Photon Source  
Argonne National Laboratory



# X-Ray Crystallography

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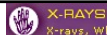
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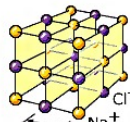


X-rays, What Are They? 6:7

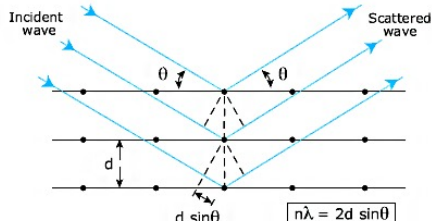
X-rays, What Are They? 7:7 >

### More About the Bragg Formula

X-rays scattered from different layers of atoms can interfere with each other. The interference depends on the wavelength of the X-ray and on the distance between the atom layers. An X-ray with well-known wavelength can be used to explore the structure of the crystal. For a well-known crystal, the X-ray properties can be examined.



Crystal planes in NaCl, ordinary salt. Other planes are also possible.



X-ray scattering from three crystal planes, separated by the distance  $d$ . For constructive interference in a direction  $\theta$  the path difference must be an even number of wavelengths.

### Related Laureates



The Nobel Prize in Physics 1915 - Sir William Henry Bragg >



The Nobel Prize in Physics 1915 - William Lawrence Bragg >

### Related Laureates



The Nobel Prize in Physics 1901 - Wilhelm Conrad Röntgen >



The Nobel Prize in Physics 1914 - Max von Laue >



The Nobel Prize in Physics 1915 - Sir William Henry Bragg >



The Nobel Prize in Physics 1915 - William Lawrence Bragg >



The Nobel Prize in Physics 1924 - Charles Glover Barkla >



The Nobel Prize in Physics 1924 - Karl Manne Georg Siegbahn >



The Nobel Prize in Physics 1927 - Arthur Holly Compton >



The Nobel Prize in Chemistry 1936 - Petrus Josephus Wilhelmus Debye >



The Nobel Prize in Chemistry 1962 - Max Ferdinand Perutz >



The Nobel Prize in Chemistry 1962 - John Cowdery Kendrew >



The Nobel Prize in Physiology or Medicine 1962 - Francis Harry Compton Crick >



The Nobel Prize in Physiology or Medicine 1962 - James Dewey Watson >



The Nobel Prize in Physiology or Medicine 1962 - Maurice Hugh Frederick Wilkins >



The Nobel Prize in Chemistry 1964 - Dorothy Crowfoot Hodgkin >



The Nobel Prize in Chemistry 1976 - William N. Lipscomb >



The Nobel Prize in Physiology or Medicine 1979 - Allan M. Cormack >



The Nobel Prize in Physiology or Medicine 1979 - Godfrey N. Hounsfield >



The Nobel Prize in Physics 1981 - Kai M. Siegbahn >



The Nobel Prize in Chemistry 1985 - Herbert A. Hauptman >



The Nobel Prize in Chemistry 1985 - Jerome Karle >



The Nobel Prize in Chemistry 1988 - Johann Deisenhofer >



The Nobel Prize in Chemistry 1988 - Robert Huber >



The Nobel Prize in Chemistry 1988 - Hartmut Michel >

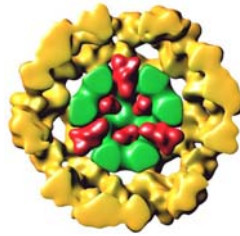
*"If a picture is worth a thousand words, then a macromolecular structure is priceless to a physical biochemist."* – van Holde



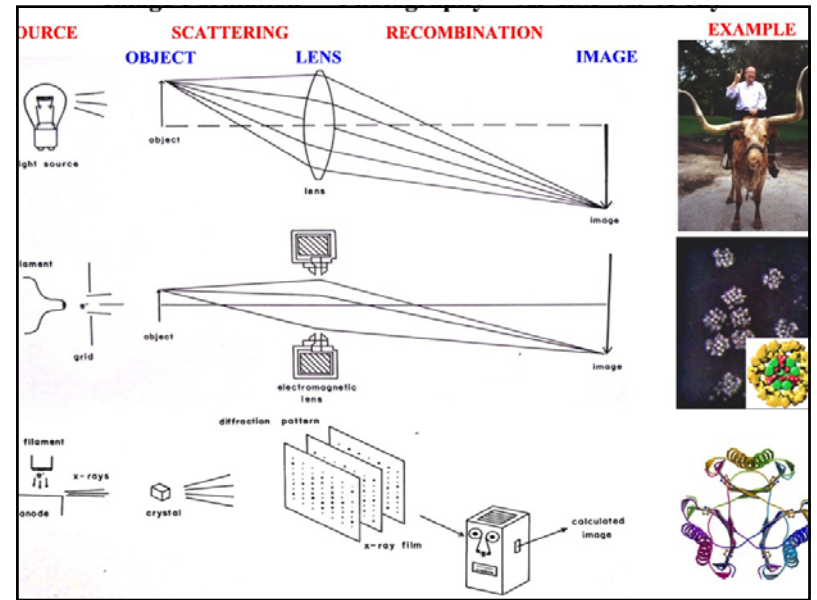
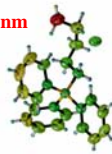
**Image Formation**  
Abbe (~1873):  
Limit Res.  $\sim \lambda/2$

• Light Photography  
 $\lambda \sim 400 - 700 \text{ nm}$

• Electron Microscopy  
 $\lambda \sim 0.001 - 0.1 \text{ nm}$

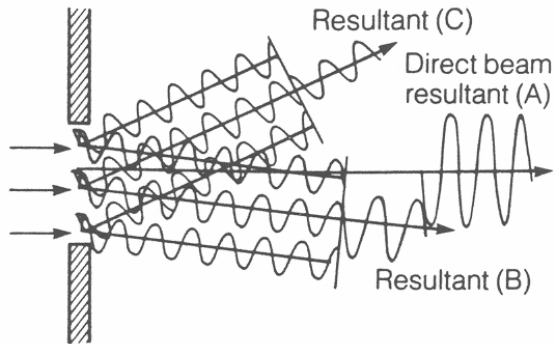


• X-Ray or NMR  
 $\lambda \sim 0.1 \text{ nm}$



### Single Hole Scattering Experiment

Transforms / Reciprocal Space

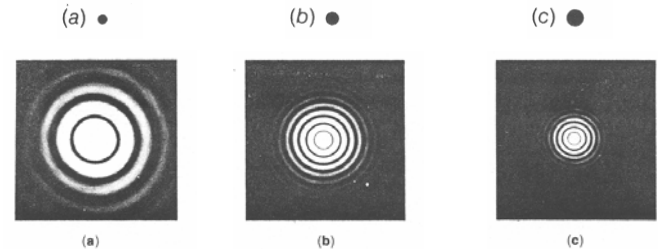


(b)

### Single Hole Scattering Experiment

Transforms / Reciprocal Space

Different size holes



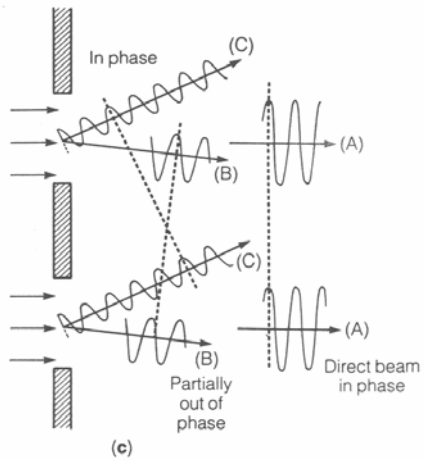
(a)

(b)

(c)

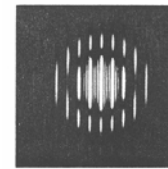
### Effect of Multiple "Scatterers"

#### Transforms / Reciprocal Space

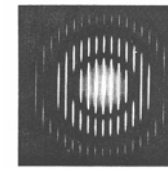


#### Transforms / Reciprocal Space

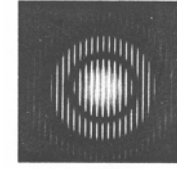
Five horizontal holes with various spacings



(j)



(k)

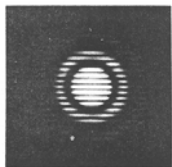


(l)

#### Transforms / Reciprocal Space

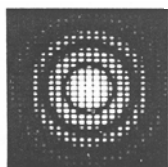
Vertical holes and nets of holes

(g)



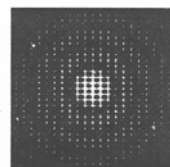
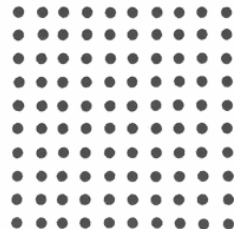
(g)

(h)



(h)

(i)

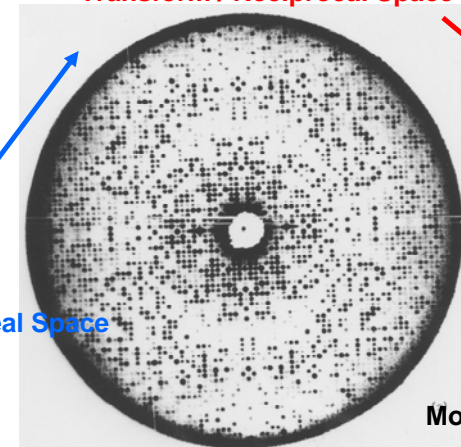


(i)

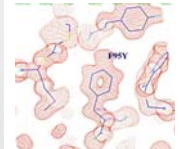
Object → Transform → Image

#### Transform / Reciprocal Space

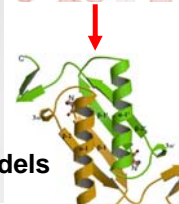
Object / Real Space



Electron Density Maps



Models




Kevin Cowtan's Picture Book of Fourier Transforms - Netscape

File Edit View Go Communicator Help

Back Forward Reload Home Search Netscape Print Security Shop Stop

Bookmarks Location <http://www.ysbl.york.ac.uk/~cowtan/fourier/fourier.html> What's Related

## Kevin Cowtan's Book of Fourier



This is a book of pictorial 2-d Fourier Transforms. These are particularly relevant to my own field of *X-ray crystallography*, but should be of interest to anyone involved in signal processing or frequency domain calculations.

**Contents:**

- [Introduction](#)
- [Book of Crystallography](#)
- [Duck Tales](#) and missing data.
- [A little Animal Magic](#) and cross phasing.
- [A Tail of Two Cats](#) and image restoration.
- [Animal Liberation](#) and free-sets.
- [The Gallery](#) Other interesting pictures.

<http://www.ysbl.york.ac.uk/~cowtan/fourier/fourier.html>

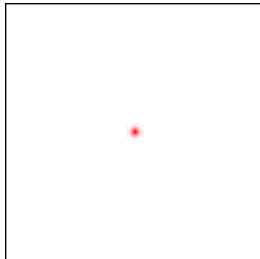
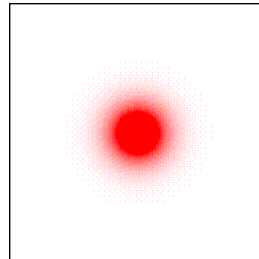
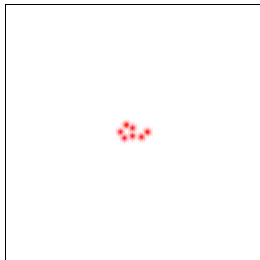
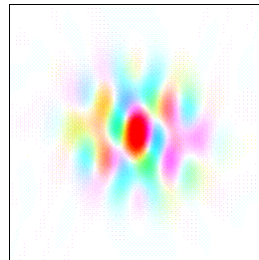
**Other topics:**

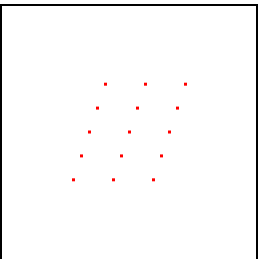
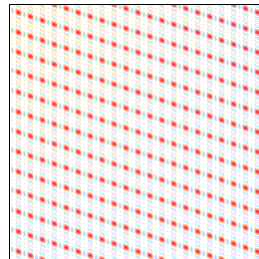
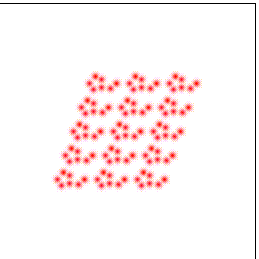
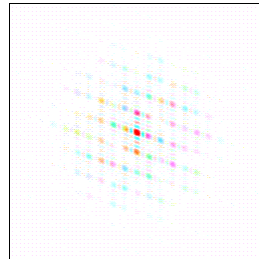
[The Interactive Structure Factor Tutorial](#) Learn about structure factors and maps.

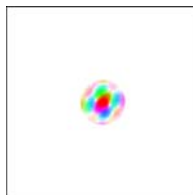
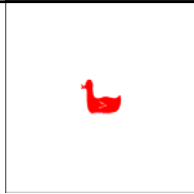
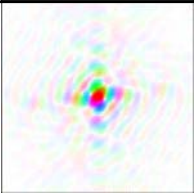
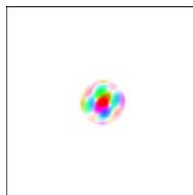
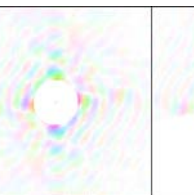
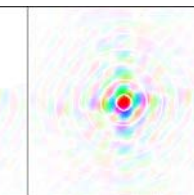
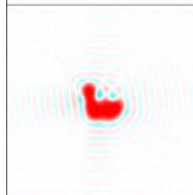

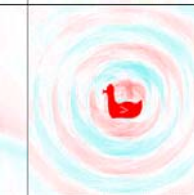
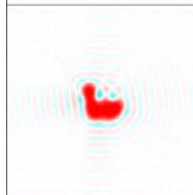

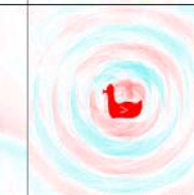
An introduction to crystallographic [Fourier transforms](#). The mathematical link between [Scattering theory](#) and Fourier theory. An explanation of the [convolution theorem](#).

**Teaching materials elsewhere**

Document: Done

Object / Real Space	Transform / Reciprocal Space
	
	

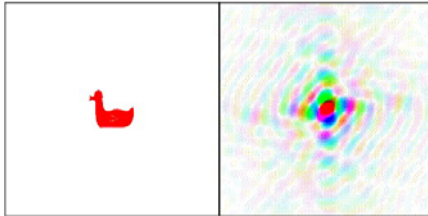
Object / Real Space	Transform / Reciprocal Space
	
	

Objects – Transforms and Image Formation	A Duck	Transform of a Duck
		
		
		
		

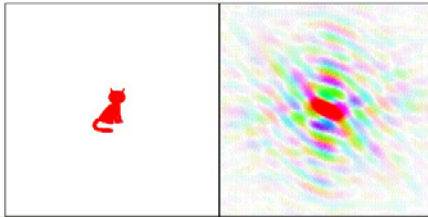
## Kevin Cowtan's Book of Fourier

<http://www.ytbl.york.ac.uk/~cowtan/fourier/fourier.html>

Here is our old friend, the Fourier Duck, and his Fourier transform:



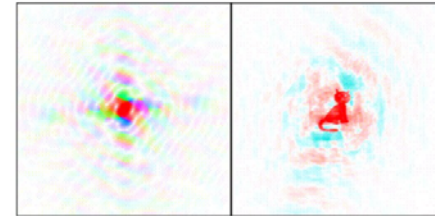
And here is a new friend, the Fourier Cat and his Fourier transform:



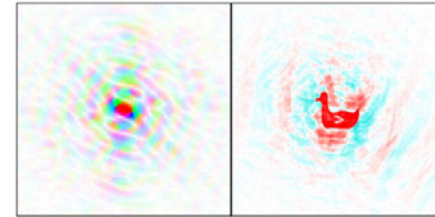
## Kevin Cowtan's Book of Fourier

<http://www.ytbl.york.ac.uk/~cowtan/fourier/fourier.html>

Duck Transform Amplitudes + Cat Phases

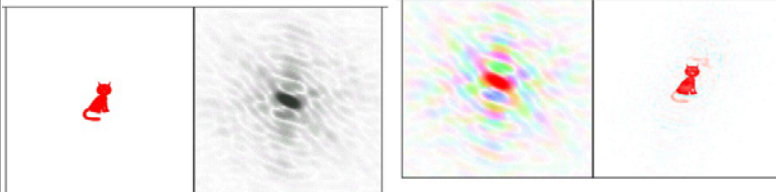


Cat Transform Amplitudes + Duck Phases



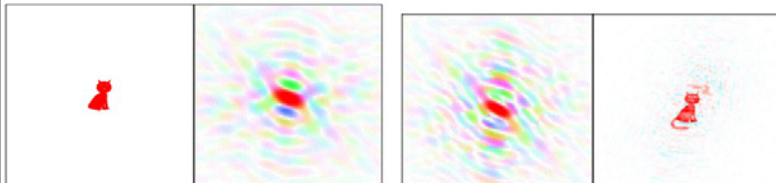
## Kevin Cowtan's Book of Fourier

<http://www.ytbl.york.ac.uk/~cowtan/fourier/fourier.html>



a) Cat - Cat Transform (Amplitudes only)  
b) Manx (tailless) Cat - Manx Transform

c) Cat Amplitudes + Manx Phases  
d)  $[2x(\text{Cat Amplitudes}) - \text{Manx Amplitudes}] + \text{Manx Phases}$



## X-Ray Crystallography

Quiz questions:

1. Crystal Growth – Materials / Methods

What is the single most important factor that determines crystal growth?

What are the two most common precipitating agents for growing protein crystals?

2. Crystal Lattices - Lattice Constants / Space Groups / Asymmetric Unit

Identify the unit cell, asymmetric unit and symmetry present in the pattern shown.



3. X-ray Sources – Sealed Tube / Rotation Anode / Synchrotron

What is responsible for “characteristic” X-rays?

What are the major advantages of using synchrotron radiation?

4. Theory of Diffraction – Bragg's Law / Reciprocal Space

When collecting an X-ray data set, what is being measured and how is that data useful?